

Model Set Questions with Answers

MODEL – 1

[CET - 501]

Full Marks – 70 Time – 3 Hours

Answer any five questions.

Figures in the right-hand margin indicate marks.

1. (a) Mention any two advantages of doubly reinforced beam. [2]
(b) Establish the comparison between working stress method and limit state method. [5]
(c) Find the depth of neutral axis of a singly reinforced RC beam of 230 mm width and 450 mm effective depth. It is reinforced with 4 bars of 16 mm diameter. Use M-20 concrete and Fe-415 bars. Use WSM and state type of beam is it. [7]
2. (a) What do you know by M-15 grade of concrete? [2]
(b) Explain the assumption in LSM of design. [5]
(c) A singly reinforced concrete beam 250 mm width is reinforced 4 bars of 25 mm diameter at an effective depth of 400 mm. If M-20 grade concrete and Fe-415 bars are used, compute ultimate moment of resistance of the section in LSM. [7]
3. (a) Define moment of Resistance. [2]
(b) State the assumptions made in limit state of collapse : Flexure. [5]
(c) A short RCC column of size 400 mm × 400 mm has to carry an axial factored load of 2000 kN. Assuming $l_{min} < 0.05 D$, design the column using M20 grade of concrete and HYSD grade of steel Fe 415. [7]
4. (a) State reasons why overreinforced section is not allowed in limit state method of design. [2]
(b) A simply supported rectangular beam (250 mm × 450 mm) reinforced with 4 nos of 16 mm dia bars as tension reinforcement is subjected to an all inclusive load of 20 kN / m over a span of 3.5 m. Design suitable shear reinforcement. The materials are M20 and Fe 415. [5]
- (c) A RCC column of dimensions 250 mm × 500 mm is reinforced with (4 – 16 + – 12) bars equally distributed on all sides. Calculate and show the details of transverse reinforcement with the help of a sketch. [7]
5. (a) What are the code provisions of stripping time for removal of props to beams? [2]
(b) A doubly reinforced beam section 250 mm wide and 450 mm deep to the centre of the tensile reinforcement. It is reinforced with 2 bars of 16 mm diameter as compressions reinforcement at an effective cover of 50 mm and 4 bars of 25 mm diameter as tensile steel. Assume M 20 concrete and Fe 415 steel. Calculate moment of resistance of the beam section. [5]
(c) Design a RCC column of the following specification using LSM.
(i) Axial factored load = 1800 kN
(ii) Effective length = 2.25 m
(iii) Grade of steel = Fe 415
(iv) Grade of concrete = M 25. [7]
6. (a) Write the purpose of providing distribution steel in RCC slabs. [2]
(b) A short RCC column 450 mm × 450 mm is provided with 8 bars of 16 mm diameter. If the effective length of the column is 2.5 m, find ultimate load for the column. Use M 20 concrete and Fe 415 steel. Solve by LSM method. [5]
(c) A RCC beam of overall dimensions 250 mm × 400 mm is subjected to a bending moment of 50 kN - m. Using M20 and Fe 415, design the section by working stress method and show details of reinforcement by a neat sketch. Assume suitable cover for mild exposure condition. [7]
7. (a) Give reasons why over reinforced section is not allowed in limit state method of design. [2]
(b) A simply supported rectangular beam (250 mm × 400 mm) reinforced with 5 nos. of 16 mm dia bars as tension reinforcement is subjected to an all inclusive load of 16 kN/m over a span of 5 m. Design for the shear reinforcement by using a

ing stress method of design and show the of main reinforcement by a neat sketch. suitable cover for moderate exposure n. [7

ANSWERS TO MODEL - 1

any two advantages of doubly reinforced beam.

higher value of factor of safety for concrete than steel because there are variations of strength of concrete due to compaction, inadequate curing, improper curing and variations in the properties of concrete.

the comparison between working stress method and limit state method.

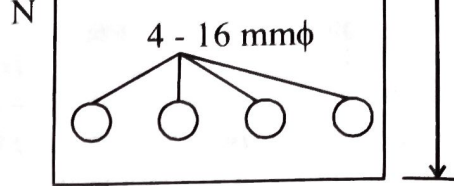
Designing the structural elements in such a way that stresses in the materials are not greater than their permissible stresses. Here the material are assumed to be elastic. The design method is known as working stress method or elastic theory of design.

Acceptable limit for the safety and serviceability requirements before failures occurs is defined as limit state. In this method of design, the structure is designed to withstand safely all loads liable throughout its life. The structure also has to meet the serviceability requirements such as deflection and cracking.

depth of neutral axis of a singly reinforced RC beam of 230 mm width and 450 mm effective depth. It is reinforced with 4 16mm diameter. Use M-20 concrete and Fe-415 bars. Use WSM and find the depth of beam is it.

M₂₀ mix, m = 13.33

$$\frac{\pi}{4}(16)^2 = 804 \text{ mm}^2$$



Let x be the depth of neutral axis.

Taking moment of transformed area about neutral axis.

$$b \cdot x \cdot \frac{x}{2} = m \cdot A_{st} (d - x)$$

$$\Rightarrow \frac{230}{2} x^2 = 13.33 \times 804 (450 - x)$$

$$\Rightarrow 115 x^2 = 4822794 - 10717 x$$

$$\Rightarrow x^2 + 93x - 41937 = 0$$

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$= \frac{-93 \pm \sqrt{8649 + 167748}}{2}$$

$$= 163 \text{ mm}$$

Depth of critical neutral axis

$$kd = 0.29 \times 450 = 130.5 \text{ mm}$$

$$x_{act} > x_{crit}$$

\therefore The beam is over-reinforced.

2.(a) What do you know by M-15 grade of concrete ?

Ans. M₂₀ means

M \rightarrow Mix.

20 \rightarrow Characteristic strength of 150 mm cube at 28 days.

(b) Explain the assumption in LSM of design.

Ans. Assumption for Designing Flexure

\Rightarrow Plane sections normal to the axis remain plane after bending.

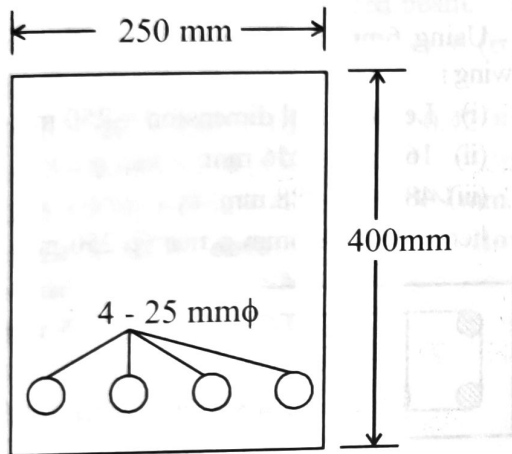
\Rightarrow The maximum strain in concrete at the outermost compression fibre is taken as 0.0035 in bending.

- ⇒ The relationship betⁿ the compressive stress distribution in concrete & the strain in concrete may be assumed to be rectangle, trapzoid, parabola or any other shape.
- ⇒ The tensile strength of the concrete is ignored.
- ⇒ The stresses in the reinforcement are derived from representative stress-strain curve for the type of steel used.
- ⇒ The maximum strain in the tension reinforcement in the section at failure shall not be less than.

$$\frac{f_y}{1.15E_s} + 0.002$$

(c) A singly reinforced concrete beam 250 mm width is reinforced 4 bars of 25 mm diameter at an effective depth of 400 mm. If M-20 grade concrete and Fe-415 bars are used, compute ultimate moment of resistance of the section in LSM.

Ans.



$$A_{st} = 4 \times 490.87 = 1963 \text{ mm}^2$$

$$\begin{aligned} \text{Total compression} &= 0.36 f_{ck} b x_u \\ &= 0.36 \times 20 \times 250 x_u = 1800 x_u. \end{aligned}$$

$$\begin{aligned} \text{Total tension} &= 0.87 f_y A_{st} \\ &= 0.87 \times 415 \times 1963 = 708741 \text{ N.} \end{aligned}$$

$$\text{Total compression} = \text{Total tension}$$

$$\Rightarrow 1800 x_u = 708741$$

$$\Rightarrow x_u = 393.7 \text{ mm}$$

$$x_{u\max} = 0.48 d = 0.48 \times 400 = 192 \text{ mm}$$

$$x_u > x_{u\max}$$

The section is over-reinforced and $x_u = 192 \text{ mm}$.

$$\begin{aligned} \text{Lever arm} = z &= d - 0.42 x_u = 400 - 0.42 \times 192 \\ &= 319.36 \text{ mm} \end{aligned}$$

$$\begin{aligned} \Rightarrow M_u &= 0.36 f_{ck} b x_u z \\ &= 0.36 \times 20 \times 250 \times 192 \times 319.36 \times 10^{-6} \text{ KNm} \\ &= 110.37 \text{ KNm.} \end{aligned}$$

3 (a) Define moment of Resistance.

Ans. Moment of resistance means couple produce when a beam subject to bending under the action of loads. It is found from the moment of inertia I and the distance from the outside of the object concerned to its major axis $W = I/c$ is used in structural.

(b) State the assumptions made in limit state of collapse : Flexure.

Ans. Refer to 2018(W), Q. No. 3.(b)

(c) A short RCC column of size 400 mm × 400 mm has to carry an axial factored load of 2000 KN. Assuming $l_{min} < 0.05 D$, design the column using M20 grade of concrete and HYSD grade of steel Fe 415.

$$\begin{aligned} \text{Ans. } A_c &= 400 \times 400 - A_{sc} \\ 2000 \times 10^3 &= 0.4 \times 20 (400 \times 400 - A_{sc}) + 0.67 \times \end{aligned}$$

$$415 A_{sc}$$

$$= 286.05 A_{sc}$$

$$\Rightarrow 720000 = 270.05 A_{sc}$$

$$\therefore A_{sc} = 2666.17 \text{ mm}^2$$

Provide 8 nos of 20mm diameter bars with

$$A_{sc} = 8 \times \frac{\pi}{4} (20)^2 = 2670 \text{ mm}^2$$

Area of concrete required for direct load

$$= \frac{2000 \times 10^3}{0.4 \times 20} = 25000 \text{ mm}^2$$

Minimum steel required

$$= \frac{0.8}{100} \times 25000 = 2000 \text{ mm}^2$$

Lateral ties

$$\phi_t = \frac{\phi}{4} = \frac{20}{4} = 5 \text{ mm} < 6 \text{ mm}$$

Use 6mmφ MS ties

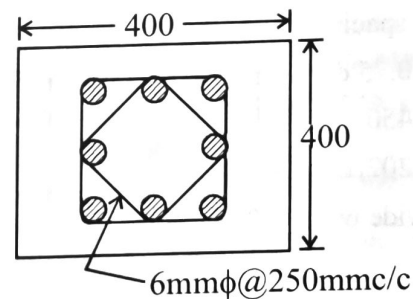
Spacing should not exceed

(i) 400 mm

(ii) $16 \times 20 = 320 \text{ mm}$

(iii) 300 mm

Use 6mm φ @ 250 mm C/C.

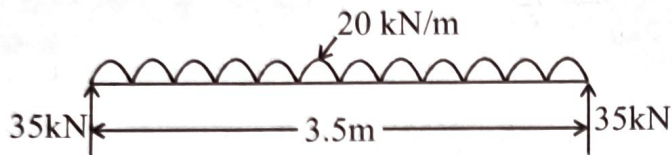


4.(a) State reasons why overreinforced section is not allowed in limit state method of design.

Ans. In case of over reinforced s/c, the steel are provided is more than that required for a balanced section. Hence, the full capacity of steel isn't utilised at same value of loads, the stresses in concrete will reach it's permissible value and fails, while stress in steel is less than it's permissible value. As concrete is a brittle material and therefore the failure is brittle and sudden. Hence over reinforced s/c isn't allowed in limit state method of design.

(b) A simply supported rectangular beam (250 mm × 450 mm) reinforced with 4 nos of 16 mm dia bars as tension reinforcement is subjected to an all inclusive load of 20 kN / m over a span of 3.5 m. Design suitable shear reinforcement. The materials are M20 and Fe 415.

Ans. Size of beam, $b = 250\text{mm}$
 $d = 450\text{ mm}$



$$v_v = \frac{V_u}{bd} = \frac{35 \times 10^3}{250 \times 450} = 6.3 \text{ N/mm}^2$$

$$A_{st} = 4 \times \frac{\pi}{4} (16)^2 = 804.24 \text{ mm}^2$$

$$P_t = \frac{A_{st}}{bd} \times 100 = \frac{100 \times 804.24}{250 \times 450} = 0.71$$

$\therefore Z_i$

$Z > Z_v < Z_{mm}$, hence safe.

Using 6mm ϕ mild steel bars for stirrups.

$A_{sv} = 2 \times 28 = 56 \text{ mm}^2$ for 2 legged vertical stirrups. Minimum spacing of stirrups.

$$S_v \leq \frac{A_{sv} f_y \times 0.87}{0.46} = \frac{56 \times 415 \times 0.87}{0.4 \times 250} = 202.18 \text{ mm}$$

The spacing can be least of

(i) $0.75 d = 0.75 \times 450 = 337.5 \text{ mm}$

(ii) 450 mm

(iii) 202.18 mm

Provide 6mm ϕ 2 legged vertical stirrup @ 200 mm C/C.

(c) A RCC column of dimensions 250 mm × 500 mm is reinforced with (4 - 16 + - 12) bars equally distributed on all sides. Calculate and show the details of transverse reinforcement with the help of a sketch.

Ans. For column size = 250mm × 500mm

$$D = 250\text{mm}$$

$$0.05 D = 0.05 \times 250 = 12.5\text{mm} \leq 20\text{mm}$$

hence provide minimum eccentricity = 20mm

$$A = 250 \times 250 = 125000 \text{ mm}^2$$

$$A_{sc} = 4 \times \frac{\pi}{4} (16)^2 + 4 \times \frac{\pi}{4} (12)^2$$

$$= 1256.63 \text{ mm}^2.$$

$$A_c = A - A_{sc} = 125000 - 1256.63 = 123743.36 \text{ mm}^2.$$

$$P_u = 0.4 f_{ck} A_c + 0.67 f_y A_{sc}$$

$$= (0.4 \times 15 \times 123743.36) + (0.67 \times 250 \times 1256.63)$$

$$= 952.94 \text{ KN.}$$

$$\text{allowable service load} = \frac{P_u}{1.5} = 635.3 \text{ KN}$$

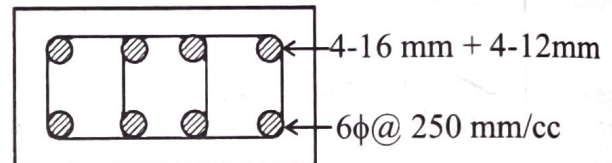
Using 6mm ϕ ties, spacing is the least of the following:

(i) Least lateral dimension = 250 mm

(ii) $16 \times 16 = 256 \text{ mm}$

(iii) $48 \times 6 = 288 \text{ mm}$

hence provide 6mm ϕ ties @ 250 mm C/C.



5.(a) What are the codal provisions of stripping time for removal of props to beams ?

Ans. Stripping time for removal of prop to beams

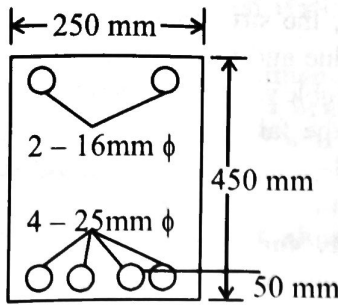
→ Spanning upto 6m = 14 days

→ Spanning over 6m = 21 days

(b) A doubly reinforced beam section 250 mm wide and 450 mm deep to the centre of the tensile reinforcement. It is reinforced with 2 bars of 16 mm diameter as compressions reinforcement at an effective cover of 50 mm and 4 bars of 25 mm diameter as tensile steel. Assume M 20 concrete and Fe 415 steel. Calculate moment of resistance of the beam section.

Ans. $f_{ck} = 20 \text{ N/mm}^2$

$f_y = 415 \text{ N/mm}^2$



Force of tension = $0.87 \sigma_y A_{st}$
 $= 0.87 \times 415 \times 4 \times 490 = 708 \text{ kN}$.

Force of compression $C = C_1 + C_2$

$C_1 = 0.36 f_{ck} b x$
 $= 0.36 \times 20 \times 250 \times (0.53 \times 400)$
 $= 381.6 \text{ kN}$.

$C_2 = (\sigma_{sc} - \sigma_{cc}) A_{sc}$
 $= (0.87 \times 415 - 0.446 \times 20) \times 2 \times \pi/4 (16)^2$
 $= 352.13 \times 402.18 = 142 \text{ kN}$.

$\therefore C = C_1 + C_2 = 523 \text{ kN}$.

Hence this is an under reinforced beam.

M.O.R = $0.36 f_{ck} b x (d - 0.42x) + (\sigma_{sa} A_{sc} - \sigma_{cc} A_{sc}) (d - d')$
 $= 0.36 \times 20 \times 250 \times 166 (400 - 0.42 \times 166)$
 $+ (0.87 \times 415 - 0.446 \times 20) (450 - 50)$
 $= (298 \times 330) + (352 \times 400) = 239 \text{ kN mm}$.

(c) Design a RCC column of the following specification using LSM.

(i) Axial factored load = 1800 kN

(ii) Effective length = 2.25 m

(iii) Grade of steel = Fe 415

(iv) Grade of concrete = M 25.

Ans. Given, Axial factored load = $P_u = 1800 \text{ kN}$.

Effective length = 2.25 m

Grade of steel $f_y = 415 \text{ N/mm}^2$

Grade of concrete $f_x = 25 \text{ N/mm}^2$

$P_u = 0.4 f_{ck} A_c + 0.67 f_y A_{sc}$

$\Rightarrow 1800 \times 10^3 = 0.4 \times 25 \times a^2 (1 - 0.008) + 0.67 \times 415 \times 0.008 a^2$
 $= 9.92 a^2 + 2.24 a^2$

$\therefore a = 385 \text{ mm}$.

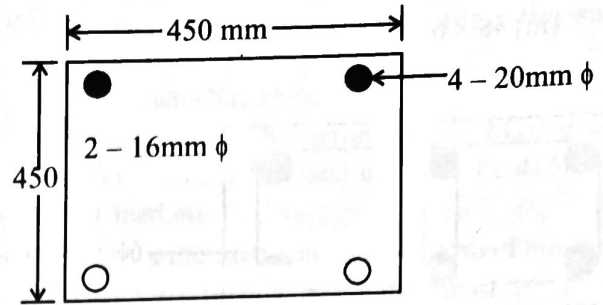
Adopt 450 mm \times 450 mm square section.

$A_g \text{ provided} = 450 \times 450 = 202500 \text{ mm}^2$

Area of conc. required = 148225 mm²

Longitudinal area of steel = $0.008 \times 148225 = 1185.8 \text{ mm}^2$.

Use 4 - 200 ϕ .



adopt 6 mm ties.

Pitch $P \leq 450 \text{ mm}$

$\leq 16 \times 20 = 320 \text{ mm}$

$\leq 300 \text{ mm}$

Adopt a pitch of 280 mm c/c.

6.(a) Write the purpose of providing distribution steel in RCC slabs.

Ans. The functions of distribution bars slabs are

→ To keep the main reinforcement in position.

→ To resist the stresses due to shrinkages and temperature.

→ To attribute uniformly the concentrated load on the slab.

(b) A short RCC column 450 mm \times 450 mm is provided with 8 bars of 16 mm diameter. If the effective length of the column is 2.5 m, find ultimate load for the column. Use M 20 concrete and Fe 415 steel. Solve by LSM method.

Ans. For column size = 450 mm \times 450 mm.

$D = 450 \text{ mm}$

$0.05 D = 0.05 \times 450 = 22.5 \text{ mm} > 20 \text{ mm}$

hence provide minimum eccentricity = 20mm.

$A = 450 \times 450 = 202500 \text{ mm}^2$

$A_{sc} = 8 \times \frac{\lambda}{4} (16)^2 = 1608.49 \text{ mm}^2$

$A_c = A - A_{sc} = 202500 - 1608.49 = 200891.5 \text{ mm}^2$

$P_u = 0.4 f_{ck} A_c + 0.67 f_y A_{sc}$

$= 0.4 \times 20 \times 200891.5 + 0.67 \times 415 \times 1608.49$
 $= 1607132 + 447215.62 = 2054 \text{ kN}$.

allowable service load = $\frac{P_u}{1.5} = 1369.5 \text{ kN}$

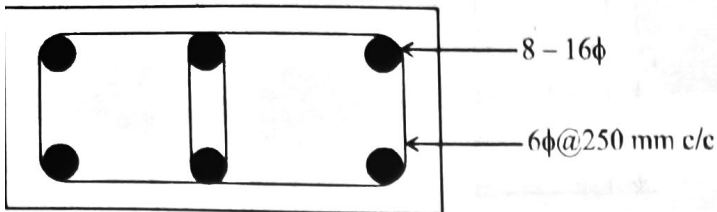
Using 6mm ϕ ties, spacing is the least of the following

(i) Least lateral dimension = 450mm.

(ii) $16 \times 16 = 256\text{mm}$

(iii) $48 \times 6 = 288\text{mm}$

hence provide 6mm ϕ ties @ 250mm c/c



(c) ARCC beam of overall dimensions 250 mm \times 400 mm is subjected to a bending moment of 50 kN - m. Using M20 and Fe 415, design the section by working stress method and show details of reinforcement by a neat sketch. Assume suitable cover for mild exposure condition.

Ans. Overall size of beam (b \times d) = 250mm \times 450mm.

For M₂₀ concrete, $\sigma_{cbc} = 7 \text{ N/mm}^2$

For Fe₄₁₅ steel, $\sigma_{st} = 230 \text{ N/mm}^2$

m = 13

For balanced section

$$K = \frac{m\sigma_{cbc}}{m\sigma_{cbc} + \sigma_{st}} = \frac{13 \times 7}{13 \times 7 + 230} = 0.283$$

$$j = 1 - \frac{k}{3} = 1 - \frac{0.283}{3} = 0.906$$

$$R = \frac{1}{2} c \cdot j \cdot k = \frac{1}{2} \times 7 \times 0.906 \times 0.283 = 0.898$$

$$\text{M.O.R.} = R \cdot b \cdot d^2 = 0.898 \times 250 \times d^2$$

$$\Rightarrow 50 \times 10^6 = 224.5 D \cdot D^2$$

$$d = \sqrt{\frac{50 \times 10^6}{224.5}} = 370 \text{ mm} \approx 395 \text{ mm}$$

Area of steel

$$\therefore A_{st} = \frac{M}{\sigma_{st} \cdot j \cdot d} = \frac{50 \times 10^6}{230 \times 0.906 \times 375} = 588 \text{ mm}^2$$

Thus provide a beam of 250mm width and 400mm effective depth with area of tensile reinforcement equal to 588 mm².

7.(a) Give reasons why over reinforced section is not allowed in limit state method of design.

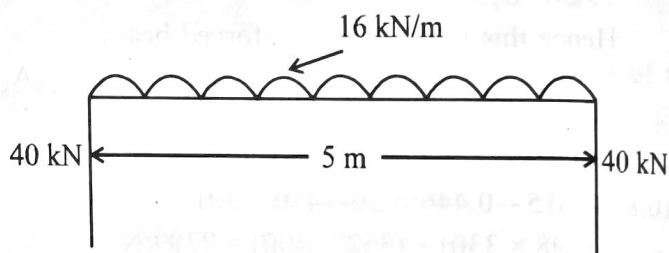
Ans. In case of over reinforced s/c, the steel are

provided is more than that required for a balanced section. Hence, the full capacity of steel isn't utilised at same value of loads, the stresses in concrete will reach its permissible value and fails, while stress in steel is less than its permissible value. As concrete is a brittle material and therefore the failure is brittle and sudden. Hence over reinforced s/c isn't allowed in limit state method of design.

(b) A simply supported rectangular beam (250 mm \times 400 mm) reinforced with 5 nos. of 16 mm dia bars as tension reinforcement is subjected to an all inclusive load of 16 kN/m over a span of 5 m. Design for the shear reinforcement by using a combination of bent up bars and vertical stirrups assuming the ends of reinforcement are confined with compressive reaction. The materials are M20 and Fe415.

Ans. Size of beam, b = 250mm

d = 400mm



$$v_v = \frac{V_u}{bd} = \frac{40 \times 10^3}{250 \times 400} = 0.4 \text{ N/mm}^2$$

$$A_{st} = 5 \times \frac{\lambda}{4} (16)^2 = 1005 \text{ mm}^2$$

$$P_t = \frac{A_{st}}{bd} \times 100 = \frac{100 \times 1005}{250 \times 400} = 1.0$$

$$\therefore \tau = 0.60$$

$$\therefore \tau > \tau_v < \tau_{max}, \text{ hence safe.}$$

$$\tau_{c \max} = 2.5 \text{ N/mm}^2 \text{ for } M_{10} \text{ concrete}$$

Using 6mm ϕ mild steel bars for stirrups

$$A_{sv} = 2 \times 28 = 56 \text{ mm}^2 \text{ for 2 legged vertical stirrups.}$$

stirrups.

Minimum spacing of stirrups

$$S_v \leq \frac{A_{sv} f_y \times 0.87}{0.4b} = \frac{56 \times 415 \times 0.87}{0.4 \times 250} = 202.18 \text{ mm}$$

The spacing can be least of

$$(i) 0.75d = 0.75 \times 400 = 300 \text{ mm}$$

- (ii) 450mm
(iii) 202.18mm

Provide 6mm ϕ two legged vertical stirrups @ 200mm c/c

- (c) A RCC beam of overall dimensions 250 mm \times 450 mm is subjected to a bending moment of 50 kNm. Using Fe 415 and M20 design the section by working stress method of design and show the details of main reinforcement by a neat sketch. Assume suitable cover for moderate exposure condition.

Ans. Overall size of beam (b \times D) = 250 mm \times 450 mm

For m_{20} concrete, $c = \sigma_{cbc} = 7 \text{ N/mm}^2$

For fe_{415} steel, $\sigma_{st} = 230 \text{ N/mm}^2$

$$m = 13$$

For a balanced section

$$K = \frac{m\sigma_{cbc}}{m\sigma_{cbc} + \sigma_{st}} = \frac{13 \times 7}{13 \times 7 + 230} = 0.283$$

$$j = 1 - k/3 = 1 - \frac{0.283}{3} = 0.906$$

$$R = \frac{1}{2} \cdot C \cdot j \cdot k = \frac{1}{2} \times 7 \times 0.906 \times 0.283 = 0.898$$

$$\text{M.O.R} = R \cdot b \cdot d^2 = 0.898 \times 250 \times d^2$$

$$\Rightarrow 50 \times 10^6 = 224.5 d^2$$

$$d = \sqrt{\frac{50 \times 10^6}{224.5}} = 470 \text{ mm} \approx 415 \text{ mm}$$

Area of steel

$$A_{st} = \frac{M}{\sigma_{std}} = \frac{50 \times 10^6}{250 \times 0.906 \times 415} = 532 \text{ mm}^2$$

This provide a beam of 250mm width and 415mm effective depth with area of tensile reinforcement equal to 532mm².

MODEL - 2

[CET - 501]

Full Marks - 70

Time - 3 Hours

Answer any five questions.

Figures in the right-hand margin indicate marks.

1. (a) Calculate the flexural strength of which grade of concrete. [2]

- (b) A rectangular R.C.C. beam of size 350 mm width \times 450 mm effective depth is reinforced with 4 nos. 16 mm diameter bars. Find the safe concentrated central point load on a simple span of 3.6 m, which the beam can carry in addition to its self-weight. The materials are M20 grade concrete and HYSD steel of grade Fe 415. Use WSD method. [5]

- (c) A simply supported rectangular beam of 5m span carries a uniformly distributed load 16 kN/m inclusive of its self weight. It also carries a central point load of 16 kN. The width of beam is 230 mm and the materials are M_{20} and mild steel reinforcement (WSM)

(i) Find the depth.

(ii) Find the steel area. [7]

2. (a) Name the grades of concrete which are used as lean concrete. [2]

- (b) A short column of size (230 \times 300) mm is reinforced with 6nos. of 16 mm dia bars. Determine the safe factored load on column. If the materials are M_{20} conc and HYSD reinforcement of grade Fe415. [5]

- (c) A rectangular beam is reinforced with 2 nos of 16 mm dia at top and 3 nos of 20 mm dia at bottom. The beam is 250 mm wide and 460 mm effective depth is subjected to a moment of 60 kN.m. Find out maximum stress developed in materials if M_{20} conc and m.s bar is used. [7]

3. (a) What is the role of concrete cover over the reinforcement? [2]

- (b) A simply supported rectangular beam over a span of 3.6 m is reinforced in tension only. The beam is 230 mm wide and had an effective depth of 510 mm. It is reinforced with 4 no. 16 mm diameter bars. Calculate the stresses in both materials at the centre span when the beam carries a uniformly distributed load of 36 kN/m inclusive of self wt. The materials are M20 grade concrete and mild steel reinforcement use WSD method. [5]

- (c) A simply supported rectangular beam of 8 m span carries a uniformly distributed load of 23 kN/m, inclusive of its self weight. Determine the reinforcement for flexure. The materials are M 30 grade concrete and TMT bars of grade Fe 415, Use LSM. [7]

4. (a) Mention the cases in which you would recommend a double reinforced beam. [2]
- (b) A tee-beam section having 230 mm width of web and 460 mm effective depth is reinforced, with 5 nos. of 16 mm dia bars as tension reinforcement which continue for a distance greater than effective depth, past the section. The section is subjected to a factored shear of 90 kN. Check the shear stresses and design the shear reinforcement. The materials used are M20 grade concrete and HYSD reinforcement of grade Fe 415. Use mild steel bars for stirrups. [5]
- (c) A doubly reinforced rectangular beam of overall size 230 mm width \times 550 mm depth is reinforced with 2 nos 20 mm diameter bars at top and 4 nos 20 mm diameter bars at bottom. If this beam is subjected to a moment of 72 kN-m, consider $d = 500$ mm, $d' = 50$ mm. Use M_{20} and Fe_{415} . Adopt working stress method.
- (i) Find the stress in concrete.
- (ii) Find the stress in comp steel.
- (iii) Find the stress in tension steel. [7]
5. (a) Where would be the critical section for which shear reinforcement is to be designed if the applied loads introduce tension in the end regions of a beam? [2]
- (b) A simply supported tee-beam of 8m clear span carries a total characteristic load of 30 kN/m. The section of the beam is 230 mm wide \times 500 mm effective depth. It is reinforced with 6 no. of 20 mm diameter bars. design the shear reinforcement using vertical stirrups only. The ends of the beam are confined by compressive reaction. The materials are M20 grade concrete and HYSD steel of grade Fe 415. Use mild steel bar of 6 mm diameter for minimum shear reinforcement. Show different section on the beam by line diagram. Use LSM. [5]
- (c) A simply supported rectangular beam of 6 m span carries a uniformly distributed characteristic load of 24 kN/m inclusive of its self-weight. The beam section is 230 \times 600 mm overall. The materials are M20 grade concrete and HYSD reinforcement of grade Fe 415. Design the beam for flexure and check for development length and deflection. Use LSM. [7]
6. (a) Calculate the effective width of flange for a continuous T beam. $l_{\text{off}} = 4.5$ m, $b_w = 300$ mm, $D_f = 130$ mm. [2]
- (b) Show that the value of neutral axis factor for flexural members by working stress method for balanced section depends only on σ_{st} (permissible stress in steel in tension). [5]
- (c) A tee beam of effective flange width of 1800 mm, thickness of slab 100 mm, width of rib 230 mm and effective depth of 500 mm is reinforced with 7 (seven) nos 28 mm diameter bars. The materials are M_{20} and Fe_{415} (Use LSM). [7]
- (i) Find actual neutral axis
- (ii) Find factored moment of resistance
- (iii) Find factored udl inclusive of its own weight assuming simply supported at both ends having effective span 4.5 m.
7. (a) Find the required cross-sectional area of column when (i) $M_U = 4000$ kN (ii) Grade = M_{20} Fe_{415} (iii) 1.0% reinforcement. [2]
- (b) A L-beam has a flange of effective width 90 cm and depth 10 cm. Determine the areas of compression and tension steels needed for the cross-section if it is to carry a factored bending moment of 600 kN-m. Assume M_{20} and Fe_{500} and use limit state method.
- (i) For determination of tension steel.
- (ii) For determination of compression steel. [5]
- (c) A short column 400 mm \times 400 mm is reinforced with 4 nos. of 25 mm diameter bars. Find the ultimate load carrying capacity of the column if the minimum eccentricity is less than .05 times the lateral dimensions. The materials are M 20 grade of concrete and Fe 415 grade of steel. Adopt limit state method. [7]

ANSWER TO MODEL - 2

1. (a) Calculate the flexural strength of which grade of concrete.

Ans. Flexural strength for $f_{cr} = 0.7\sqrt{f_{ck}}$

For M_{20} grade of concrete

$$f_{cr} = 0.7\sqrt{20} = 3.1305 \text{ N/mm}^2$$

- (b) A rectangular R.C.C. beam of size 350 mm width \times 450 mm effective depth is reinforced

with 4 nos. 16 mm diameter bars. Find the safe concentrated central point load on a simple span of 3.6 m, which the beam can carry in addition to its self-weight. The materials are M20 grade concrete and HYSD steel of grade Fe 415. Use WSD method.

Ans. For M20 grade concrete, $\sqrt{c_{bc}} = 7 \text{ N/mm}^2$

$$m = \frac{280}{3\sqrt{c_{bc}}}$$

$$\Rightarrow m = \frac{280}{3 \times 7} = 13.3$$

$$A_{st} = 4 \times \frac{\pi}{4} \times 16^2 = 804 \text{ mm}^2$$

Let x be the depth of neutral axis. Taking moment of transformed areas about NA.

$$350 \times \frac{\pi^2}{2} = 13.33 \times 804 (450 - x)$$

$$\Rightarrow x^2 = 27558.82 - 61.24$$

$$\text{or, } x^2 + 61.24 \times -27558.82 = 0$$

$$\text{Which gives } x = 138.19 \text{ mm}$$

$$\text{Depth of critical NA} = 0.29 \times 450 = 130.5 \text{ mm.}$$

$$x_{\text{actual}} > x_{\text{critical}}$$

\therefore Section is over reinforced and concrete will fail first.

$$MR = \frac{1}{2} \cdot \sigma_{c_{bc}} \cdot b \cdot x \left(d - \frac{x}{3} \right)$$

$$= \frac{1}{2} \times 7 \times 350 \times 138.19 \left(450 - \frac{138.19}{3} \right)$$

$$= 68.40 \text{ kNm.}$$

$$\text{Self wt of beam} = 0.35 \times 0.500 \times 25 \times 3.6 = 15.75 \text{ kN.}$$

If load on beam is WKN.

$$M = \frac{w\ell}{2} = 68.40$$

$$W = 38 \text{ kN.}$$

$$\therefore \text{Additional safe concentrated load on beam} = 38 - 15.75 = 22.25 \text{ kN.}$$

(c) A simply supported rectangular beam of 5m span carries a uniformly distributed load 16 kN/m inclusive of its self weight. It also carries a central point load of 16 kN. The

width of beam is 230 mm and the materials are M₂₀ and mild steel reinforcement (WSM)

(i) Find the depth.

(ii) Find the steel area.

$$\text{Ans. } M = \frac{\omega\ell^2}{8} + \frac{W\ell}{4}$$

$$= \frac{16 \times 5^2}{8} + \frac{16 \times 5}{4}$$

$$= 70 \text{ kNm.}$$

$$m = \frac{280}{3 \times \delta_{c_{bc}}} = \frac{280}{3 \times 7} = 13.33$$

$$Q_{bal} = 1.21$$

$$\text{Effective depth required} = \sqrt{\frac{M}{Q_{bal} \times b}}$$

$$= \sqrt{\frac{70 \times 10^6}{1.21 \times 230}}$$

$$= 501.5 \text{ MM} >$$

$$A_{s_{bal}} = \frac{M}{\delta_{st} j d}$$

$$= \frac{70 \times 10^7}{140 \times 0.87 \times 501.5} = 1146 \text{ MM}^2$$

2.(a) Name the grades of concrete which are used as lean concrete.

Ans. The grade of concrete below M₁₀ is used as lean concrete.

(b) A short column of size (230 × 300) mm is reinforced with 6nos. of 16 mm dia bars. Determine the safe factored load on column. If the materials are M₂₀ conc and HYSD reinforcement of grade Fe415.

Ans. Size of column = 230 × 300

using 6 nos. 16 mm # bar

$$A_{sc} = 1206 \text{ mm}^2$$

$$A_c = \text{gross area} - A_{sc}$$

$$= (230 \times 300) - 1206$$

$$= 67794 \text{ mm}^2$$

using M₂₀ conc.s F_{c415} steel

$$f_{ck} = 20 \text{ N/mm}^2$$

$$f_y = 415 \text{ N/mm}^2$$

Assume minimum eccentricity is less than $0.5D$, $I_{\min} = 20 \text{ mm}$.

$$P_u = 0.4 f_{ck} A_c + 0.67 f_y A_{sc}$$

$$= (0.4 \times 415 \times 67794) + (0.67 \times 415 \times 1206) \times$$

$$10^{-6}$$

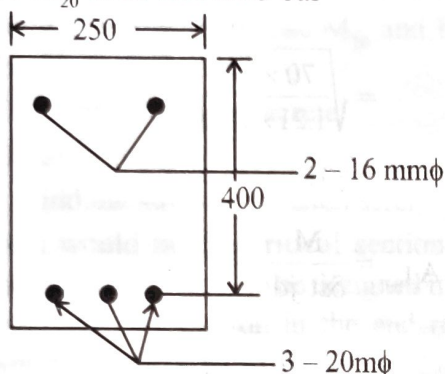
$$= 11.59 \text{ KN.}$$

- (c) A rectangular beam is reinforced with 2 nos of 16 mm dia at top and 3 nos of 20 mm dia at bottom. The beam is 250 mm wide and 460 mm effective depth is subjected to a moment of 60 kN.m. Find out maximum stress developed in materials if M_{20} conc and m.s bar is used.

Ans. $b = 250 \text{ mm}$

$d = 460 \text{ mm}$

use M_{20} conc and M.S bar



$f_{ck} = 20 \text{ N/mm}^2$

$f_y = 250 \text{ N/mm}^2$

Bending moment = 60 kN. m

Factor Moment = $1.5 \times 60 = 90 \text{ KN m}$.

2 nos. of 16 mm ϕ at top

So, $A_{sc} = 402 \text{ mm}^2$.

3 nos of 20 mm ϕ at bottom.

$A_{st} = 942 \text{ mm}^2$.

$M_u = 90 \text{ KN m}$.

$$M_{u\lim} = 0.36 f_{ck} b d^2 \frac{X_{u\max}}{d} \left(1 - 0.42 \frac{X_{u\max}}{d} \right)$$

$$= 0.36 \times 20 \times 250 \times (460)^2 \times 0.53 (1 - 0.42 \times$$

$$0.53) \times 10^{-6}$$

$$= 156.93 \text{ KNm.}$$

- 3.(a) What is the role of concrete cover over the reinforcement ?

Ans. A concrete cover is provided to the reinforcement for the following reasons

(1) To protect the reinforcement from weather and fire, so that it does not corrode or melt.

(2) To ensure the grip of concrete over reinforcement so that they act as one and resist the loads.

- (b) A simply supported rectangular beam over a span of 3.6 m is reinforced in tension only. The beam is 230 mm wide and had an effective depth of 510 mm. It is reinforced with 4 no. 16 mm diameter bars. Calculate the stresses in both materials at the centre span when the beam carries a uniformly distributed load of 36 kN/m inclusive of self wt. The materials are M20 grade concrete and mild steel reinforcement use WSD method.

Ans. For M20 mix, $m = 13.3$

$$A_{st} = 4 \times 201 = 804 \text{ mm}^2$$

Transformed area of steel = $m A_{st}$

$$= 13.33 \times 804 = 10717 \text{ mm}^2$$

To find neutral axis, taking moments of transformed areas about neutral axis.

$$230 \frac{x^2}{2} = 10717(510 - x)$$

$$\Rightarrow x^2 = 47527.56 - 53.19x$$

$$\Rightarrow x^2 = 53.19x - 47527.56 = 0$$

$$x = 193.02 \text{ mm}$$

For the beam,

Maximum moment at centre = $\frac{wl^2}{8}$

$$= \frac{36 \times 3.6^2}{8} = 58.72 \text{ KNM.}$$

Lever arm = $510 - \frac{193.02}{3} = 445.66 \text{ mm}$.

Steel stress $f_{st} = \frac{58.72 \times 10^6}{804 \times 445.66} = 163.88 \text{ N/mm}^2$

Concrete stress $f_{cb} = \frac{f_{st}}{m} \times \frac{x}{d - x}$

$$= \frac{163.88}{13.33} \times \frac{193.02}{510 - 193.02} = 5.48 \text{ N/mm}^2$$

- (c) A simply supported rectangular beam of 8 m span carries a uniformly distributed load of 23 kN/m, inclusive of its self weight.

Shot on VIVO Z1X

Determine the reinforcement for flexure. The materials are M 30 grade concrete and TMT bars of grade Fe 415, Use LSM.

Ans. For Fe 415 grade reinforcement

$$\frac{M_{ulim}}{f_{ck} b d^2} = 0.138$$

$$\text{and } \frac{P_{tlim} f_y}{f_{ck}} = 19.68$$

For M30 grade concrete

$$Q_{lim} = 0.138 \times 30 = 4.14$$

$$P_{tlim} = \frac{19.86 \times 30}{415} = 1.44$$

Maximum bending moment

$$M = 23 \times \frac{8^2}{8} = 184 \text{ KNM}$$

Ultimate bending moments

$$M_u = 1.5 \times 184 = 276 \text{ KNM.}$$

Adopt $b = 250 \text{ mm.}$

$$\text{Balanced depth, } Q_{lim} = \frac{M_u}{b d^2}$$

$$\Rightarrow d = \sqrt{\frac{276 \times 10^6}{4.14 \times 250}} = 516.4 \text{ mm}$$

Assume 10% larger depth and 60 mm effective cover.

$$D = 1.1 \times 516.4 + 60 = 628 \text{ mm.}$$

$$\text{Use } D = 650 \text{ mm } d = 650 - 60 = 590 \text{ mm}$$

$$\frac{M_u}{b d^2} = \frac{276 \times 10^6}{250 \times 590^2} = 3.17$$

$$P_f = 50 \left[\frac{1 - \sqrt{1 - \frac{4.6}{30} \times 3.17}}{\frac{415}{30}} \right] = 1.02$$

$$A_{st} = \frac{1.02}{100} \times 250 \times 590 = 1505 \text{ mm}^2$$

$$A_{st \text{ lim}} = \frac{1.44}{100} \times 250 \times 590 = 2124 \text{ mm}^2$$

$$\text{Provide } 5 - 20\# = 5 \times 314 = 1570 \text{ mm}^2$$

$$A_{st \text{ required}} < A_{st \text{ provide}} < A_{st \text{ lim}} \dots \dots \dots (\text{ok})$$

4.(a) Mention the cases in which you would recommend a double reinforced beam.

Ans. For a design moment M , if the size of the rectangular section is fixed and the moment of resistance of a singly reinforced section is less than M , a double reinforced beam is recommended.

(b) A tee-beam section having 230 mm width of web and 460 mm effective depth is reinforced, with 5 nos. of 16 mm dia bars as tension reinforcement which continue for a distance greater than effective depth, past the section. The section is subjected to a factored shear of 90 kN. Check the shear stresses and design the shear reinforcement. The materials used are M20 grade concrete and HYSD reinforcement of grade Fe 415. Use mild steel bars for stirrups.

$$\text{Ans. } V_u = 90 \text{ KN, } b = 230 \text{ MM } d = 460 \text{ MM}$$

$$\text{Nominal shear stress, } \tau_v = \frac{V_u}{b \times d}$$

$$\tau_v = \frac{90 \times 10^3}{230 \times 460} = 0.85 \text{ N/MM}^2 < 2.8 \text{ N/MM}^2$$

Where 2.8 N/MM^2 is the maximum nominal shear stress for M20 Mix.

$$\frac{100A_s}{bd} = \frac{100 \times 1005}{230 \times 460} = 0.95$$

For $\frac{100A_s}{bd} = 0.95$, τ_c shall be calculated by interpolation.

$$\text{For } \frac{100A_s}{bd} = 0.75, \tau_c = 0.56 \text{ N/MM}^2$$

$$\text{For } \frac{100A_s}{bd} = 1.00, \tau_c = 0.62 \text{ N/MM}^2$$

$$\therefore \text{For } \frac{100A_s}{bd} = 0.95$$

$$\tau_c = 0.56 + \frac{0.62 - 0.56}{1 - 0.75} (0.95 - 0.75)$$

$$= 0.608 \text{ N/MM}^2$$

Now $\tau_v > \tau_c$, therefore shear reinforcement shall be designed.

Shear resistance of concrete

$$V_{uc} = \tau_c b d = 0.608 \times 230 \times 460 \times 10^{-3} = 64.3 \text{ kN}$$

Shear to be resisted by stirrups

$$V_{us} = V_u - V_{uc} = 90 - 64.3 = 25.7 \text{ KN}$$

Using 6MM diameter two-legged stirrups

$$A_{sv} = 56 \text{ MM}^2$$

$$S_v = \frac{0.87 f_y A_{sv} d}{V_{us}} = \frac{0.87 \times 250 \times 56 \times 460}{25.7 \times 10^3} = 218 \text{ MM}$$

or by using equation.

$$S_v = \frac{0.87 \times f_y \times A_{sv}}{b(\tau_v - \tau_c)}$$

$$= \frac{0.87 \times 2.50 \times 56}{230(0.85 - 0.608)} = 218 \text{ MM}$$

The spacing shall not exceed

(i) $0.75 d = 0.75 \times 460 = 345 \text{ MM}$

(ii) 300 MM

(iii) due to minimum shear reinforcement required

i.e 132.4 MM

(iv) required spacing = 218 MM

∴ Provide 6 MM ϕ two-legged stirrups about 130

MM c/c.

(c) A doubly reinforced rectangular beam of overall size 230 mm width \times 550 mm depth is reinforced with 2 nos 20 mm diameter bars at top and 4 nos 20 mm diameter bars at bottom. If this beam is subjected to a moment of 72 kN-m, consider $d = 500 \text{ mm}$, $d' = 50 \text{ mm}$. Use M_{20} and F_{e415} . Adopt working stress method.

(i) Find the stress in concrete.

(ii) Find the stress in comp steel.

(iii) Find the stress in tension steel.

Ans. For M 20 grade concrete $m = 13.33$

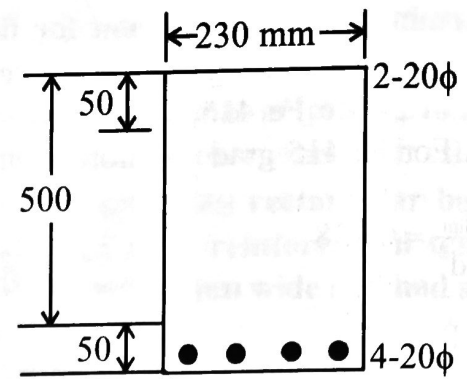
$$\text{Compression steel } A_{sc} = 2 \times \frac{\pi}{4} \times 20^2 = 628 \text{ MM}^2$$

$$\text{Transformed area} = (105 \times 13.33 - 1) \times 628 = 11938 \text{ MM}^2$$

$$\text{Tension steel} = 4 \times \frac{\pi}{4} \times 20^2 = 1256 \text{ MM}^2$$

$$\text{Transformed area} = 13.33 \times 1256 = 16750 \text{ MM}^2$$

To find the position of neutral axes taking moments of transformed areas about NA



$$\frac{1}{2} \times 230 x^2 + 11938(x - 50) = 16750(500 - x)$$

$$\Rightarrow 115x^2 + 28688x - 8971900 = 0$$

$$\Rightarrow x^2 + 249.5x - 78016.5 = 0$$

which gives $x = 181.2 \text{ MM}$.

$$\text{Now } x_{\text{critical}} = 0.29 \times 500 = 145 \text{ MM}.$$

$$x_{\text{actual}} > x_{\text{critical}}$$

∴ Section is overreinforced and concrete will fail first.

Taking moments of compressive forces about tensile steel and equating to the external BM

$$M = (1.5m - 1)A_{sc} \times \frac{x - d'}{x} f_{cb} (d - d')$$

$$+ bx \frac{f_{cb}}{2} \left(d - \frac{x}{3} \right)$$

$$\Rightarrow 70 \times 10^6 = (1.5 \times 13.33 - 1) \times 628$$

$$\times \left(\frac{181.2 - 50}{181.2} \right) \times f_{cb} (500 - 50) + 230$$

$$\times 181.2 \times \frac{f_{cb}}{2} \left(500 - \frac{181.2}{3} \right)$$

$$= 13048162.28 f_{cb}$$

$$\Rightarrow f_{cb} = 5.36 \text{ N / MM}^2$$

0 Stress in compression steel

$$F_{sc} = 1.5m \left(\frac{x - d}{x} \right) f_{cb}$$

$$= 1.5 \times 13.33 \left(\frac{181.2 - 50}{181.2} \right) \times 5.36$$

$$= 77.6 \text{ N / MM}^2$$

N / MM^2
 would be the critical section for which reinforcement is to be designed if the loads introduce tension in the end of a beam?

applied loads introduce tension in the beam the shears computed at the face will be used in the design of the member.

supported tee-beam of 8m clear span total characteristic load of 30 kN/m. Section of the beam is 230 mm wide and effective depth. It is reinforced with 20 mm diameter bars. design reinforcement using vertical stirrups only. The ends of the beam are fixed by compressive reaction. The concrete is M20 grade concrete and HYSD grade Fe 415. Use mild steel bar of 20 mm diameter for minimum shear reinforcement. Show different section on the shear force diagram. Use LSM.

load = 30 kN/m
 dead load = $1.5 \times 30 = 45$ kN/m
 shear force,

$$\frac{1}{2} \times 45 \times 8 = 180 \text{ kN.}$$

$$\frac{180 \times 10^3}{230 \times 500} = 1.56 \text{ N/mm}^2$$

$m^2.$

stirrups

$$(20)^2 = 1884 \text{ mm}^2$$

$$\frac{1800 \times 1884}{230 \times 500} = 1.64$$

N/mm^2

$$S_v = \frac{0.4b}{0.4 \times 230} = 392 \text{ mm}$$

$$S_v > 300 \text{ mm}$$

$$> 0.75 \times 500 = 375 \text{ mm, which ever is smaller.}$$

$$\text{i.e. } S_v = 300 \text{ mm}$$

Provide 8 mm # 2 legged stirrups @ 300 mm c/c

Shear resistance,

$$V_{usmin} = \frac{0.87f_y A_{sv} d}{S_v} = \frac{0.87 \times 415 \times 100 \times 500 \times 10^{-3}}{300}$$

$$= 60.2 \text{ kN.}$$

$$\text{Total shear resistance} = 84.7 + 60.2 = 144.9 \text{ kN.}$$

At the face of the support is considered.

$$V_u = 180 \text{ kN, } \tau_v = 1.56 \text{ N/mm}^2, \tau_c = 0.737 \text{ N/mm}^2$$

$$\tau_v > \tau_c$$

Thus shear design is necessary

$$V_{uc} = 84.7 \text{ kN, } V_{us} = 180 - 84.7 = 95.3 \text{ kN.}$$

Using 8 mm # 2 legged vertical stirrup.

$$S_v = \frac{0.87f_y A_{sv} d}{V_{us}} = \frac{0.87 \times 415 \times 100 \times 500}{95.3 \times 10^3} = 189 \text{ mm}$$

The spacing should not exceed.

$$(i) 392 \text{ mm}$$

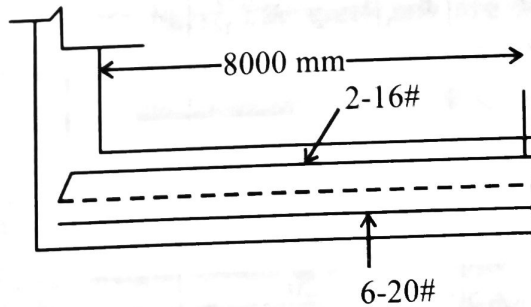
$$(ii) 0.75d = 0.75 \times 500 = 375 \text{ mm}$$

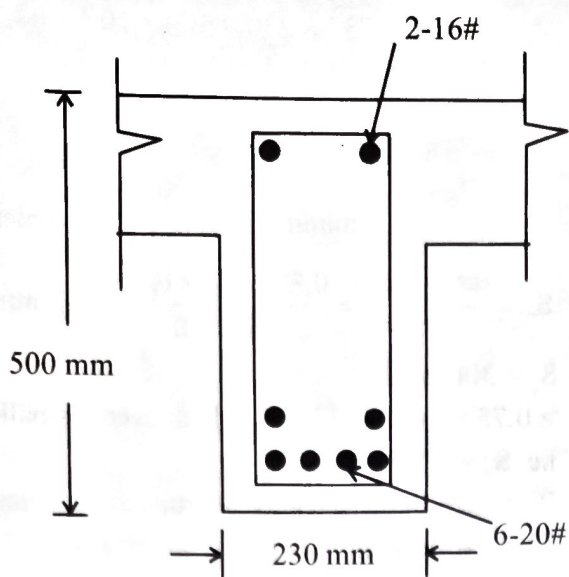
$$(iii) 300 \text{ mm.}$$

Provide 8 mm # @ 180 mm c/c stirrups at support

continue the same spacing upto 780 mm.

$$\text{No. of stirrups} = \frac{780}{180} + 1 = 6 \text{ nos.}$$





(c) A simply supported rectangular beam of 6 m span carries a uniformly distributed characteristic load of 24 kN/m inclusive of its self-weight. The beam section is 230 × 600 mm overall. The materials are M20 grade concrete and HYSD reinforcement of grade Fe 415. Design the beam for flexure and check for development length and deflection. Use LSM.

Ans. Factored load = $1.5 \times 24 = 36$ kN/m.

$$M_u = \frac{36 \times 6^2}{8} = 162 \text{ kNm}$$

$$V_u = \frac{36 \times 6}{8} = 108 \text{ kN}$$

(a) Moment steel

Assuming 20 mm diameter bars in one layer
 $d = 600 - 30 - 10 = 560$ mm.

$$\frac{M_u}{bd^2} = \frac{162 \times 10^6}{230 \times 560^2} = 2.25 < 2.76$$

∴ The section is singly reinforced.

$$P_t = 50 \left[\frac{1 - \sqrt{1 - \frac{4.6}{f_{ck}} \times \frac{M_u}{bd^2}}}{f_y / f_{ck}} \right]$$

$$= 50 \left[\frac{1 - \sqrt{1 - \frac{4.6}{20} \times 2.25}}{415/20} \right] = 0.74$$

$$A_{st} = \frac{0.74}{100} \times 230 \times 560 = 953 \text{ mm}^2$$

$$A_{st \text{ lim}} = \frac{0.96}{100} \times 230 \times 560 = 1236 \text{ mm}^2$$

Provide 2.20 # 2.16 # = $2(314 + 201) = 1030 \text{ mm}^2$.

Let 2.16 # bars are bent a $1.25 D = 1.25 \times 600 = 750$ mm, from the face of the support.

The remaining bars should extend within the support for a distance of

$$\frac{L_d}{3} = \frac{1}{3} \times 47 \times 20 = 313 \text{ mm}$$

(b) Check for development length

(1) A bar can be bent up at a distance greater than $L_d = 47 \#$ from the centre of the support, i.e. $47 \times 16 = 752$ mm.

In this case this distance $(3000 - 750) = 2250$ mm.

(2) For the remaining bars $A_{st} = 2 \times 314 = 628 \text{ MM}^2$.

$$M_{ulin} = 0.87 f_y A_{st} d \left(1 - \frac{f_y A_{st}}{f_{ck} b d} \right)$$

$$= 0.87 \times 415 \times 628 \times 560$$

$$\left(1 - \frac{415 \times 628}{20 \times 230 \times 560} \right) \times 10^{-6}$$

$$= 114.12 \text{ kNm}$$

$$V_u = 108 \text{ kN}, L_0 = 12\# \text{ (assume)}$$

As the reinforcement is confined by compressive reaction

$$1.3 \frac{M_{ul}}{V_u} + L_0 \geq L_d$$

$$\therefore 1.3 \times \frac{114.12 \times 10^6}{108 \times 10^3} + 12\# \geq 47\# \quad 39.2 \geq \#$$

provided = 20 MM (Safe)

The remaining bars should extend within the

support for a distance of $\frac{L_d}{3} = \frac{1}{3} \times 47 \times 20 = 313 \text{ MM}$.

If support width is 300 mm, the bars extends for $150 + L_0 = 150 + 12 \times 20 = 390 \text{ mm}$ within the support.

(c) Check for deflection

Basic

$$\frac{\text{span}}{d} \text{ ratio} = 20 \text{ (for simply supported beam)}$$

$$\text{Service stress} = 0.58 \times f_y \times \frac{A_{st \text{ required}}}{A_{st \text{ pro}}}$$

$$= 0.58 \times 4.15 \times \frac{936}{1030}$$

$$= 219 \text{ N/mm}^2$$

$$\frac{100A_{st}}{bd} = \frac{100 \times 1030}{230 \times 560} = 0.8$$

$$\text{Modification factor} = 1.15$$

$$\frac{\text{Span}}{d} \text{ permissible} = 20 \times 1.15 = 23$$

$$\text{Actual } \frac{\text{Span}}{d} = \frac{6000}{565} = 10.62 \text{ (safe)}$$

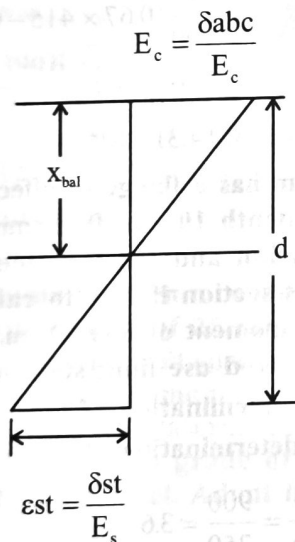
- 6.(a) Calculate the effective width for flange for a continuous T beam. $l_{\text{eff}} = 4.5 \text{ m}$, $b_w = 300 \text{ mm}$, $D_f = 130 \text{ mm}$.

$$\text{Ans. } b_f = \frac{l_0}{6} + 6D_f + b_w$$

$$= \frac{4.5 \times 10^3}{6} + 6 \times 130 + 300 = 1830 \text{ mm}$$

- (b) Show that the value of neutral axis factor for flexural members by working stress method for balanced section depends only on σ_{st} (permissible stress in steel in tension).

$$\text{Ans. } \frac{X_{\text{bal}}}{d - X_{\text{bal}}} = \frac{\epsilon_c}{\epsilon_{st}}$$



$$= \frac{\delta abc}{E_c} = \frac{M \delta abc}{\delta st E_s}$$

Solving for X_{bal}

$$X_{\text{bal}} = \left(\frac{M \delta abc}{M \delta abc + \delta st} \right) d$$

$$= \left[\frac{1}{1 + \frac{\delta st}{M \delta abc}} \right] d$$

Substituting $M = \frac{280}{3 \delta abc}$

$$X_{\text{bal}} = \left[\frac{1}{1 + \frac{\delta st}{\frac{280}{3 \delta abc \times \delta abc}}} \right] d = k d$$

Where k is known as neutral axis constant.

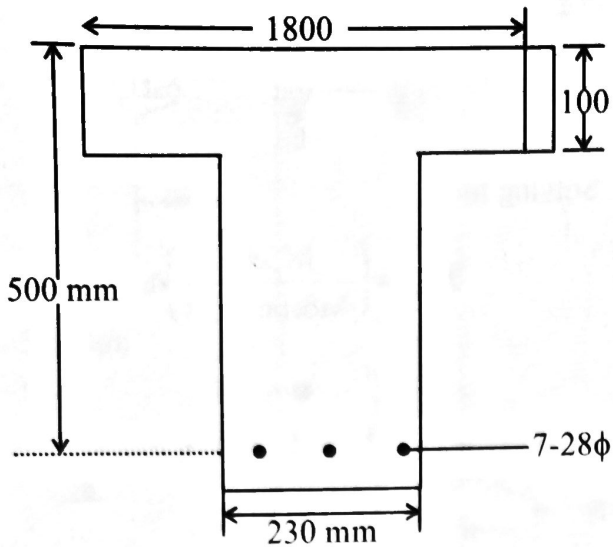
$$k = \frac{1}{1 + \frac{\delta st}{\frac{280}{3}}} = \frac{1}{1 + 0.0107 \delta st}$$

This shows that the value of constant k does not depend on grade of concrete but on the permissible stress in steel.

- (c) A tee beam of effective flange width of 1800 mm, thickness of slab 100 mm, width of rib 230 mm and effective depth of 500 mm is reinforced with 7 (seven) nos 28 mm diameter bars. The materials are M_{20} and Fe_{415} (Use LSM).

- (i) Find actual neutral axis
- (ii) Find factored moment of resistance
- (iii) Find factored udl inclusive of its own weight assuming simply supported at both ends having effective span 4.5 m.

Ans.



$$A_{st} = 7 \times \frac{\pi}{4} \times 28^2 = 4310 \text{ MM}^2$$

Assuming NA to fall in flange, we have

$$\frac{X_u}{d} = \frac{0.87 f_y A_{st}}{36 f_{ck} b_{fd}} = 0.240$$

$$x_u = 0.24 \times 500 = 120 \text{ MM} > D_f$$

Hence NA falls outside flange

To obtain a new value of X_u equate compressive force to tensile force

$$T_u = 0.87 f_y A_{st} = 1556125.5 \text{ N}$$

$$y_t = 0.15 x_u + 0.65 D_t = 83 > D_t$$

$$C_u = 0.36 f_{ck} x_u b_w + 0.446 f_{ck} (b_f - b_w) y_f$$

$$= 0.36 \times 20 \times x_u \times 230 + 0.446 \times 20 (1800 - 230)$$

$$(0.15 x_u + 0.65 D_t)$$

$$= 1656 x_u + 14004.4 (0.15 x_u + 65)$$

$$= 3756.66 x_u + 910586$$

$$\text{Equating, } T_u \text{ and } C_u$$

$$1556125.5 = 3756.66 x_u + 910286$$

$$\Rightarrow X_u = 171.92 \text{ MM.}$$

$$X_{u \max} = 0.48 \times d = 240 \text{ MM} > x_u$$

$$\text{Now } \frac{3}{7} x_u = 73.68 < D_f$$

$$y_f = 0.15 x_c + 0.65 D_f$$

$$= 0.15 \times 171.92 + 65$$

$$= 90.8 \text{ MM.}$$

$$M_u = 0.36 f_{ck} b_w x_u (d - 0.42 x_u)$$

$$+ 0.446 f_{ck} (b_f - b_w) y_f \times \left(D_f - \frac{y_f}{2} \right)$$

$$= 0.36 \times 20 \times 230 \times 171.92 (500 - 0.42$$

$$\times 171.92) + 0.446 \times 20 (1800 - 230)$$

$$\times 90.8 \left(100 - \frac{90.8}{2} \right)$$

$$= 191.22 \text{ kNm.}$$

Let W_u = Factored udl inclusive of its own weight

$$\Rightarrow M_u = \frac{\omega_u l^2}{8}$$

$$\Rightarrow 191.22 = \frac{\omega_u \times 4.5^2}{8}$$

$$\Rightarrow \omega_u = 75.6 \text{ kN / M}$$

- 7.(a) Find the required cross-sectional area of column when (i) MU = 4000 kN (ii) Grade = M_{20} Fe₄₁₅ (iii) 1.0% reinforcement.

$$\text{Ans. } \frac{P_u}{A_g} = 0.4 f_{ck} + \frac{P}{100} (0.67 f_y - 0.4 f_{ck})$$

$$\Rightarrow \frac{4000 \times 10^3}{A_g} = 0.4 \times 20$$

$$+ \frac{1}{100} (0.67 \times 415 - 0.4 \times 20)$$

$$= 10.7005$$

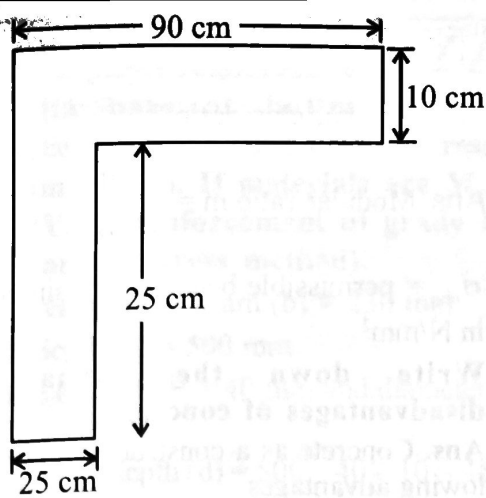
$$\Rightarrow A_g = 373814.31 \text{ MM}^2.$$

- (b) A L-beam has a flange of effective width 90 cm and depth 10 cm. Determine the areas of compression and tension steels needed for the cross-section if it is to carry a factored bending moment of 600 kN-m. Assume M_{20} and Fe₅₀₀ and use limit state method.

(i) For determination of tension steel. [4

(ii) For determination of compression steel. [3

$$\text{Ans. } \frac{b_f}{b_w} = \frac{900}{250} = 3.6$$



$$\frac{D_f}{d} = \frac{\omega_0}{(350 - 40)} = 0.32$$

Assuming effective tension cover = 40 MM.

$$\frac{M_{ulim}}{f_{ck} b_w d^2} = 0.417$$

$$\Rightarrow M_{ulim} = 0.417 \times 20 \times 250 \times 310^2 = 200.4 \text{ kNM.}$$

$$A_{st1} = \frac{M_{ulim}}{0.87 \times f_y \left(d - \frac{D_f}{2} \right)}$$

$$= \frac{200.4 \times 10^6}{0.87 + 500 \left(310 - \frac{100}{2} \right)}$$

$$= 1771.9 \text{ MM}^2$$

$$M_2 = 600 - 200.4 = 399.6 \text{ kNM}$$

$$A_{st2} = \frac{399.6 \times 10^6}{0.87 \times 500 + (310 - 40)}$$

$$= 3402.3 \text{ MM}^2$$

$$A_{st} = A_{st1} + A_{st2} = 5174.2$$

(c) A short column 400 mm × 400 mm is reinforced with 4 nos. of 25 mm diameter bars. Find the ultimate load carrying capacity of the column if the minimum eccentricity is less than .05 times the lateral dimensions. The materials are M 20 grade of concrete and Fe 415 grade of steel. Adopt limit state method.

Ans. Size of column = 400 mm × 400 mm

$$A_{st} = 4 \times \frac{\pi}{4} \times 25^2 = 1962 \text{ mm}^2$$

$$\text{Area of concrete} = 160000 - 1962.5 = 158037.5 \text{ mm}^2.$$

e_{min} does not exceed $0.5 \times b$

$$P_u = 0.4 f_{ck} \cdot A_c + 0.67 f_y \times A_{st}$$

$$= 0.4 \times 20 \times 158037.5 + 0.67 \times 415 \times 1962.5$$

$$= 1809973.125 \text{ N} = 1809.97 \text{ KN.}$$

MODEL - 3

[CET - 501]

Full Marks - 70

Time - 3 Hours

Answer any five questions.

Figures in the right-hand margin indicate marks.

1. (a) What is modular ratio? [2]
- (b) Write down the advantages and disadvantages of concrete. [5]
- (c) A singly reinforced beam (230 × 500) mm overall depth is reinforced with 3 nos. of 20 mm dia bars at bottom as tension reinforcement. Find out moment of resistance of beam section. If materials are M₂₀ conc and HYSD reinforcement of grade FE415 (use working stress method). [7]
2. (a) Define the characteristic strength of material. [2]
- (b) A simply supported beam (250 × 500) mm overall depth is reinforced with 4 nos. of 20 mm dia as tension reinforcement. The beam is subjected to factored shear of 100kN at support. Check the shear stress and design the 6mm dia vertical stirrups at support. The materials are M₂₀ conc. and m.a. reinforcement. [5]
- (c) Design a simple supported singly reinforced beam of 230 mm wide which carries a factored load of 30 kN/m including its self weight. The span of beam is 6m. Design the beam for flexure and shear by limit state method if materials are M₁₅ conc and HYSD bars of Fe415. [7]
3. (a) What do you mean by M₂₀ mix? [2]
- (b) A rectangular beam is reinforced with 2 nos of 16 mm dia at top and 3 nos of 20 mm dia at bottom. The beam is 250 mm wide and 460 mm effective depth is subjected to a moment of 60 kN.m. Find out maximum stress developed in materials if M₂₀ conc and m.s bar is used. [5]
- (c) Design a simply supported Tee beam of span 6m and spaced at 3m centres. The thickness of slab

ANSWER TO MODEL - 3

- is 120 mm and total factored load including self weight of beam is 45 kN/m. Design the beam for flexure and shear if materials are M_{20} conc. and HYSD bars of grade Fe415. [7]
- 4.(a) What do you mean by balanced design ? [2]
- (b) A singly reinforced beam (230 × 500) mm overall depth is reinforced with 3 nos. of 20 mm dia bars at bottom as tension reinforcement. Find out moment of resistance of beam section. If materials are M_{20} conc and HYSD reinforcement of grade FE415 (use working stress method). [5]
- (c) A short RCC column has to carry an axial factored load of 2000 kN. Design the column by using M_{15} grade conc and m.s. reinforcement. [7]
- 5.(a) What do you mean by diagonal tension and diagonal compression. [2]
- (b) A rectangular beam of size (250 × 560) mm effective depth is subjected to a factored moment of 220kN.m. Find the reinforcement for flexure if the materials are M_{20} conc and HYSD reinforcement of grade Fe415. [5]
- (c) Design a two-way restrained slab for an office floor carrying a live load of 2.5 kN/m². The slab is 4.5 m × 5.5 m from centre to centre of beam and two adjacent edges are discontinuous. Use M_{15} conc and mild steel bars. [7]
- 6.(a) What are the advantages of two way slab over one way slab. [2]
- (b) A.R.C. beam has an effective depth of 500 mm and a breadth of 350 mm. It contains 4-25 mm bars. Calculate the shear reinforcement needed for a factored shear force of 350 kN. Adopt limit state method and design and assume M_{15} grade of concrete and Fe 415 grade of steel. [5]
- (c) Design a slab for a room measuring 5.5 × 4 m assuming superimposed load of 3 kN/m². The slab is supported on 300 mm thick walls on all four sides and is simply supported at edges with no provision to resist torsion at corners. HYSD reinforcement of grade Fe 415 L.S.M. of design. [7]
- 7.(a) Mention the value of partial safety factor for concrete and steel. [2]
- (b) What are the assumptions made in the design for flexure in working stress method ? [5]
- (c) A short RCC column has to carry an axial factored load of 2000 kN. Design the column by using M_{15} grade conc and m.s. reinforcement. [7]

1.(a) What is modular ratio ?

$$\text{Ans. Modular ratio } m = \frac{280}{3\sigma_{cbc}}$$

σ_{cbc} = permissible bending stress in compression in N/mm²

(b) Write down the advantages and disadvantages of concrete.

Ans. Concrete as a construction material entails the following advantages.

Advantage

1. It has high compressive strength and corrosive and weathering effects are minimal. Its strength is equal to that of a hard material stone when properly prepared.
2. As compared to other materials concrete is economical in the long run.
3. It is durable and fire resistant and requires very little maintenance.
4. The green concrete can be easily handled and moulded into any shape or size according to specification.
5. The concrete can be pumped and hence it can be laid in difficult positions.
6. Concrete can even be sprayed on and filled into the cracks for repair by grouting process.
7. It has unlimited application in combination with steel reinforcement.

Disadvantage

Following are the disadvantages

1. Concrete is reinforced with steel bars since it has low tensile strength and hence cracks easily.
2. Provision of construction joints has to be made to avoid development of cracks due to drying shrinkage and moisture movement in fresh concrete.
3. In order to avoid the formation of cracks due to thermal movement concrete expands and contracts with the change of temperature. Expansion joints have to be provided.
4. Concrete as a material lacks in ductility and this factor provides disadvantages with respect to earthquake resistance design.
5. Concrete is liable to disintegrate by alkaline and sulphate attack.
6. Concrete undergoes creep under sustained loading resulting in reduction of prestress in the prestressed concrete construction.

(c) A singly reinforced beam (230 × 500) mm overall depth is reinforced with 3 nos. of 20 mm dia bars at bottom as tension reinforcement. Find out moment of resistance of beam section. If materials are M₂₀ conc and HYSD reinforcement of grade FE415 (use working stress method).

Ans. breadth of the beam (b) = 230 mm

overall depth (c) = 500 mm.

Assume clearcover = 40 mm and diameter of bar = 20 mm

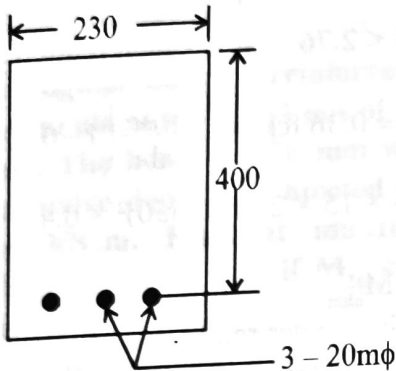
So, effective depth (d) = 500 - 40 - 10 = 450 mm.

M₂₀ φ Fe₄₁₅ materials used.

$\sigma_{cbc} = 7 \text{ N/mm}^2$.

$$\text{So, } F_{ck} = 20 \text{ N/mm}^2 M = \frac{280}{3 \times \sigma_{cbc}}$$

$$= \frac{280}{3 \times 7} = 13.3$$



$\sigma_{cbc} = 7 \text{ N/mm}^2$

$\sigma_{st} = 230 \text{ N/mm}^2$

3 nos 20 mm dia bars are used $A_{st} = 942 \text{ mm}^2$

By transformed area method

$$b \times x \times \frac{x}{2} = M.A_{st}(d - x)$$

$$\Rightarrow 230 \times \frac{x^2}{2} = 13.33 \times 942(450 - x)$$

$$\Rightarrow 115x^2 = 5650587 - 12556.86x$$

$$\Rightarrow x^2 - 491355.5 - 12556.86x$$

$$\Rightarrow x^2 + 109.49x - 49135.5 = 0$$

$$\Rightarrow x = 173.67 \text{ mm.}$$

$$\text{But } X_{cr} = \frac{1}{1 + \frac{\sigma_{st}}{m\sigma_{cbc}}} \times d$$

$$K = \frac{1}{1 + \frac{\sigma_{st}}{m\sigma_{cbc}}} = \frac{1}{1 + \frac{230}{13.33 \times 7}} = 0.29$$

$$x_{cr} = 0.29 \times 450 = 130.5 \text{ mm}$$

$$X_{\text{actual}} > X_{\text{critical}}$$

So, this is a over-reinforced Beam.

$$M.R = \frac{1}{2} \sigma_{cbc} \times x \left(d - \frac{x}{3} \right) \times b$$

$$= \frac{1}{2} \times 7 \times 173.7 \left(450 - \frac{173.7}{3} \right) \times 230 \times 10^{-6}$$

$$= 54.82 \text{ kN.m.}$$

2.(a) Define the characteristic strength of material.

Ans. Characteristic Compressive Strength

It means that value of the strength of the materials below which not more than 5% of the test result are expected to fail.

M₁₅ grade of conc and Fe₂₅₀ is used

So, $\sigma_{cbc} = 5 \text{ M/mm}^2$

$$m = \frac{280}{3 \times 5} = 18.67$$

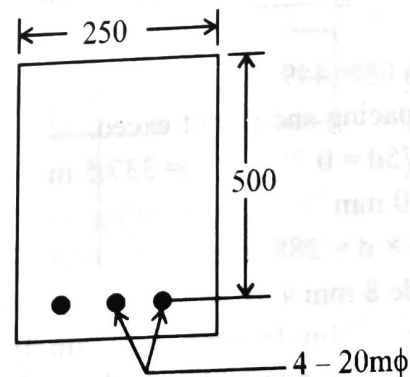
(b) A simply supported beam (250 × 500) mm overall depth is reinforced with 4 nos. of 20 mm dia as tension reinforcement. The beam is subjected to factored shear of 100kN at support. Check the shear stress and design the 6mm dia vertical stirrups at support. The materials are M₂₀ conc. and m.a. reinforcement.

Ans. Data given

b = 250 mm.

D = 500 mm

Using 4 - 20 mm φ bar.



$$A_{st} = 1257 \text{ mm}^2$$

Assume clear cover = 40 mm.

$$\text{Effective depth } (d) = 500 - 40 - 10 = 450 \text{ mm.}$$

$$\text{Factor shear force} = 100 \text{ kN} = V_u$$

Using M_{15} and M.S Bar

$$\text{So, } f_{ck} = 15 \text{ N/mm}^2$$

$$f_y = 250 \text{ N/mm}^2$$

$$\frac{100A_s}{bd} = \frac{100 \times 1257}{250 \times 450} = 1.11$$

$$\tau_c = 0.67 \text{ N/mm}^2 \text{ (15456 T - 19)}$$

$$\tau_u = \frac{V_u}{bd} = \frac{100 \times 10^3}{250 \times 450} = 0.89 \text{ N/mm}^2$$

$$\tau_u > \tau_c.$$

Shear design is necessary

$$V_u = \tau_{cbd} = 0.67 \times 250 \times 450 = 75375 = 75.375 \text{ KN.}$$

$$V_{us} = V_u - V_{uc} \\ = 100 - 75.375 = 24.625 \text{ kN.}$$

Using 6 mm 4 legged stirrups with $A_{sv} = 113 \text{ mm}^2$.

$$S_v = \frac{0.87 f_y A_{svo}}{V_{us}} \\ = \frac{0.87 \times 250 \times 113 \times 450}{24.625 \times 10^3}$$

$$= 449 \text{ mm}$$

Spacing is least of following

(i) 449 mm

(ii) $0.75 \times 450 = 337.5 \text{ mm}$ i.e. 300 mm

Provide 6 mm 4 legged stirrup @ 300 mm C/C

$$V_{us \text{ min}} = \frac{0.87 f_y A_{sv} d}{S_v} \\ = \frac{0.87 \times 250 \times 113 \times 450}{300} \\ = 449 \text{ mm.}$$

The spacing shows not exceed.

$$(1) 0.75d = 0.75 \times 450 = 337.5 \text{ mm}$$

$$(2) 300 \text{ mm}$$

$$(3) 48 \times d = 288 \text{ mm.}$$

Provide 8 mm # @ 280 C/C stirrup at support

(c) Design a simple supported singly reinforced beam of 230 mm wide which carries a factored

load of 30 kN/m including its self weight. The span of beam is 6m. Design the beam for flexure and shear by limit state method. Materials are M_{15} conc and HYSD bars of Fe415.

Ans. Width of the beam (b) = 230 mm $f_{ck} = 15 \text{ KN/mm}^2$.

(∴ M_{15} con)

factor load = 30 KN/m

Span of the beam = 6m.

$$\text{Factor Moment} = \frac{ML^2}{8} = \frac{30 \times (6)^2}{8} \\ = 138 \text{ KN/m.}$$

$$\text{Assume } D = \frac{\text{Span}}{10} = 600 \text{ mm}$$

$$\frac{M_u}{bd^2} = \frac{138 \times 10^2}{230 \times (550)^2} \quad d = 600 - 50 = 550 \text{ mm}$$

$$= 1.98 < 2.76 \text{ - It is single reinforced beam.}$$

$$M_{u \text{ lim}} = 0.36 f_{ck} b d^2 \frac{X_{u \text{ max}}}{d} \left(1 - 0.42 \frac{X_{u \text{ max}}}{d} \right) \\ = 0.36 \times 15 \times 230 \times (550)^2 \times 0.48 \times (1 - 0.42 \times 0.48) \times 10^{-6}$$

$$M_u < M_{u \text{ lim}}$$

So, it is a under reinforced beam

Steel calculation

$$M_u = 0.87 f_y A_{st} d \left(1 - \frac{f_y A_{st}}{b d f_{ck}} \right)$$

$$\Rightarrow 138 \times 10^6 = 0.87415 \times A_{st} \times 550 \left(1 - \frac{415 A_{st}}{230 \times 550 \times 15} \right)$$

$$\Rightarrow 138 \times 10^6 = 198577.5 A_{st} - 43.43 A_{st}^2$$

$$\Rightarrow A_{st}^2 - 45722.28 A_{st} + 3177527 = 0$$

$$\Rightarrow A_{st} = 3717 \text{ mm}^2$$

Provide 25 mm 8 nos

A_{st} provided = 3927 mm^2 .

Design for shear

$$\text{Maximum shear} = \frac{wL}{2}$$

$$= \frac{138 \times 6}{2} = 414 \text{ KN}$$

$$\tau_v = \frac{V_u}{bd} = \frac{414 \times 10^3}{230 \times 550} = 3.2 \text{ N/mm}^2$$

$$\frac{100A_s}{bd} = \frac{100 \times 3922}{230 \times 550} = 3.1$$

$$\tau_c = 0.71 \text{ N/mm}^2 (15456 - T - 19)$$

$$\tau_v = \tau_c$$

Minimum Stirrup

Use 6 mm 2 legged stirrup $A_{st} = 56 \text{ mm}^2$

$$S_v = \frac{0.87 f_y A_{sv}}{0.4b} = 219 \text{ mm}$$

- Spacing is minimum of the following (i) 219 mm,
- (ii) $1.75d = 412.5 \text{ mm}$ (iii) 300 mm (iv) $48 \times 6 = 288 \text{ mm}$
- S_v 6 mm 2 legged stirrup @ 280 mm C/C

3.(a) What do you mean by M_{20} mix?

Ans. M_{20} means

$M \rightarrow$ Mix.

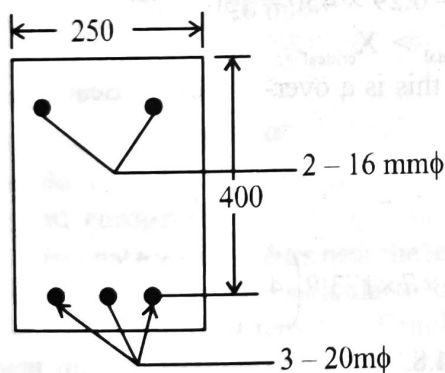
20 \rightarrow Characteristic strength of 150 mm cube at 28 days.

- (b) A rectangular beam is reinforced with 2 nos of 16 mm dia at top and 3 nos of 20 mm dia at bottom. The beam is 250 mm wide and 460 mm effective depth is subjected to a moment of 60 kN.m. Find out maximum stress developed in materials if M_{20} conc and m.s bar is used.

Ans. $b = 250 \text{ mm}$

$d = 460 \text{ mm}$

use M_{20} conc and M.S bar



$f_{ck} = 20 \text{ N/mm}^2$

$f_y = 250 \text{ N/mm}^2$

Bending moment = 60 kN.m

Factor Moment = $1.5 \times 60 = 90 \text{ KN m}$.

2 nos. of 16 mm ϕ at top

So, $A_{sc} = 402 \text{ mm}^2$.

3 nos of 20 mm ϕ at bottom.

$A_{st} = 942 \text{ mm}^2$.

$M_u = 90 \text{ KN m}$.

$$M_{ucim} = 0.36 f_{ck} b d^2 \frac{X_{u,max}}{d} \left(1 - 0.42 \frac{X_{u,max}}{d} \right)$$

$$= 0.36 \times 20 \times 250 \times (460)^2 \times 0.53 \left(1 - 0.42 \times 0.53 \right) \times 10^{-6}$$

$$= 156.93 \text{ KNm}$$

- (c) Design a simply supported Tee beam of span 6m and spaced at 3m centres. The thickness of slab is 120 mm and total factored load including self weight of beam is 45 kN/m. Design the beam for flexure and shear its materials are M_{20} conc. and HYSD bars of grade Fe415.

Ans. $t = 15 \text{ cm}$

$b_r = 30 \text{ cm}$

Span of slab = 3.5 m

left of beam = 6m

super imposed load of slab = 5 kN/m²

Overall depth of beam = $\frac{1}{12}$ to $\frac{1}{20}$ of the span.

Provide over all depth = 450 mm

Provide 20 mm bar at clear cover of 25 mm

Effective cover to reinforcement = 35 mm

Effective depth = 450 mm - 35 mm = 415 mm

Load from slab = $5000 \times 3.5 = 17500 \text{ N/m}$

D.L. of the rib = $25000 \times .3 \times .3 = 2250 \text{ N/m}$

Total load 19750 N/m

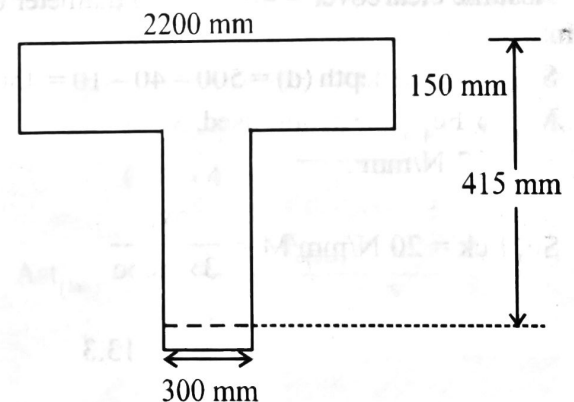
Factored load = $1.5 \times 19750 = 29625 \text{ N/m}$

$$M_u = \frac{29625 \times 6^2}{8} = 133312.5 \text{ N/m}$$

Width of flange

$$B = \frac{L}{6} + b_r + 6t$$

$$= \frac{6000}{6} + 300 + 6 \times 150 = 2200 \text{ mm}$$



$$\frac{M_u}{Bd^2} = \frac{133312.5 \times 1000}{2200 \times 415^2}$$

$$\frac{133312500}{78895000} = .352$$

Percentage of steel

$$P = 50 \left(\frac{\left(1 - \sqrt{1 - \frac{4.6}{20} \times .352} \right)}{250/15} \right)$$

$$= \frac{50 \times .0413}{16.67} = 0.124\%$$

$$P = 100 \frac{A_{st}}{Bd}$$

$$A_{st} = \frac{0.124 \times 2200 \times 415}{100} = 1132 \text{ mm}^2$$

Provide 4 bar of 20 mm (1256 mm²)

4.(a) What do you mean by balanced design ?

Ans. Balanced section.

The section is so proportioned that the steel and concrete both reach their maximum permissible values of stresses at the same time.

(b) A singly reinforced beam (230 × 500) mm overall depth is reinforced with 3 nos. of 20 mm dia bars at bottom as tension reinforcement. Find out moment of resistance of beam section. If materials are M₂₀ conc and HYSD reinforcement of grade FE415 (use working stress method).

Ans. breadth of the beam (b) = 230 mm

overall depth (c) = 500 mm.

Assume clearcover = 40 mm and diameter of bar

= 20 mm

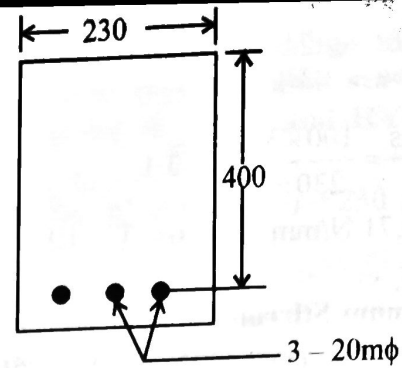
So, effective depth (d) = 500 - 40 - 10 = 450 mm.

M₂₀ φ Fe₄₁₅ materials used.

σ_{cbc} = 7 N/mm².

$$\text{So, } F_{ck} = 20 \text{ N/mm}^2 M = \frac{280}{3 \times \sigma_{cbc}}$$

$$= \frac{280}{3 \times 7} = 13.3$$



$$\sigma_{cbc} = 7 \text{ N/mm}^2$$

$$\sigma_{st} = 230 \text{ N/mm}^2$$

3 nos 20 mm dia bars are used $A_{st} = 942 \text{ mm}^2$

By transformed area method

$$b \times x \times \frac{x}{2} = M \cdot A_{st} (d - x)$$

$$\Rightarrow 230 \times \frac{x^2}{2} = 13.33 \times 942 (450 - x)$$

$$\Rightarrow 115x^2 = 5650587 - 12556.86x$$

$$\Rightarrow x^2 - 491355.5 - 12556.86x$$

$$\Rightarrow x^2 + 109.49x - 49135.5 = 0$$

$$\Rightarrow x = 173.67 \text{ mm.}$$

$$\text{But } X_{cr} = \frac{1}{1 + \frac{1 \cdot \sigma_{st}}{m \sigma_{cbc}}} \times d$$

$$K = \frac{1}{1 + \frac{\sigma_{st}}{m \sigma_{cbc}}} = \frac{1}{1 + \frac{230}{13.33 \times 7}} = 0.29$$

$$x_{cr} = 0.29 \times 450 = 130.5 \text{ mm}$$

$$X_{actual} > X_{critical}$$

So, this is a over-reinforced Beam.

$$M.R = \frac{1}{2} \sigma_{cbc} \times x \left(d - \frac{x}{3} \right) \times b$$

$$= \frac{1}{2} \times 7 \times 173.7 \left(450 - \frac{173.7}{3} \right) \times 230 \times 10^{-6}$$

$$= 54.82 \text{ kN.m.}$$

(c) A short RCC column has to carry an axial factored load of 2000 kN. Design the column by using M₁₅ grade conc and m.s. reinforcement.

Ans. Axias load = 2000 KN.

Assume $e_{min} < 05 \times D$

But $e_{min} = 20 \text{ mm}$

Therefore the min side of the colⁿ

$$= \frac{20}{0.50} = 400 \text{ mm}$$

colⁿ size = 400×400

Assume 0.8% steel.

$A_{sc} = 0.008 A_g$

$A_c = A_g. A_{sc} = 0.992 A_g$

$P_u = 0.4 f_{ck} A_c + 0.67 f_y A_{sc}$.

$$\Rightarrow 2000 \times 10 = (0.4 \times 15 \times 0.992 A_g) + (0.67 \times 250 \times 0.008 A_g)$$

$$= 5.952 A_g + 1.34 A_g$$

$$= 7.292 A_g$$

$$\Rightarrow A_g = 274273 \text{ mm}^2$$

So one side of the column = 530 mm.

i.e. size of the colⁿ = 530×530

$P_u = 0.4 f_{ck} A_c + 0.67 f_y A_{sc}$.

$$\Rightarrow 2000 \times 10^3 = \{0.4 \times 15\}$$

$$(530 \times 530 - A_{sc}) + (0.67 \times 250 \times A_{sc})$$

$$= 1685400 - 6 A_{sc} + 167.5 A_{sc}$$

$$\Rightarrow A_{sc} = 1948 \text{ mm}^2$$

$$A_c = (530 \times 530) - 1948$$

$$= 278952 \text{ mm}^2$$

$A_{sc} = 1948 \text{ mm}^2$.

Provid = $8 - 20\phi$ Asc provid = 2513 mm^2

Lateral ties.

Use 6mm ϕ latures ties

Spacing should not exceed

(i) 530 mm

(ii) $16\phi = 16 \times 20 = 320 \text{ mm}$

(iii) 300 mm

(iv) $48 \times 6 = 288 \text{ mm}$

So 6 mm ϕ ties at 280 C/C.

5.(a) What do you mean by diagonal tension and diagonal compression.

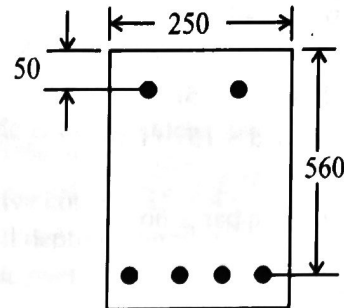
Ans. Diagonal tension occurs near the tension face tensile crack in the direction perpendicular to local tensile stress are known as diagonal tension. Crack occur in high moment diagonal compression failure occur in column. It is perp to comp stress.

(b) A rectangular beam of size (250 × 560) mm effective depth is subjected to a factored moment of 220kN.m. Find the reinforcement for flexure if the materials are M_{20} conc and HYSD reinforcement of grade Fe415.

Ans. Data given

$b = 250 \text{ mm}$

$d = 560 \text{ mm}$



Factored Bending Moment = 220 KN.M

Using M_{20} conc. H_{YSD} Bar

So, $f_{ck} = 20 \text{ N/mm}^2$.

$f_y = 415 \text{ N/mm}^2$

$M_{u1} = 220 \text{ KN.m}$.

$$M_{ucm} = 0.36 f_{ck} b d^2 \frac{X_{u,max}}{d} \left(1 - 0.42 \frac{X_{u,max}}{d} \right)$$

$$= 0.36 \times 20 \times 250 \times (560)^2 \times 0.48 (1 - 0.42 \times 0.48) \times 10^{-6}$$

$$= 216.32 \text{ KN.M}$$

$$M_u > M_{ucm}$$

So this is a doubly reinforced beam.

Assume $d^1 = 50 \text{ mm}$

$$\frac{d^1}{d} = \frac{50}{560} = 0.08 = 0.1$$

So $f_{sc} = 353 \text{ N/mm}^2$

$M_{u1} = 220 \text{ KN.m}$

$M_{ucim} = 216.32 \text{ KN.m}$

$M_{u2} = 220 - 216.32 = 3.68 \text{ KN.m}$.

$$A_{sc} = \frac{M_{u2}}{f_{sc}(d - d^1)} = \frac{3.68 \times 10^6}{353(560 - 50)} \times 20.40 \text{ mm}^2$$

$$A_{st2} = \frac{A_{sc} f_{sc}}{0.87 f_y}$$

$$= \frac{20.40 \times 353}{0.87 \times 415} = 20 \text{ mm}^2$$

$$A_{st(lim)} = \frac{M_{u(lim)}}{0.87 f_y d \left(1 - 0.42 \times \frac{X_{u,max}}{d} \right)}$$

$$= \frac{216.32 \times 10^6}{0.87 \times 415 \times 560 (-0.42 \times 0.48)}$$

$$= 1340 \text{ mm}^2$$

$$A_{st} = 1340 + 20 = 1360 \text{ mm}^2$$

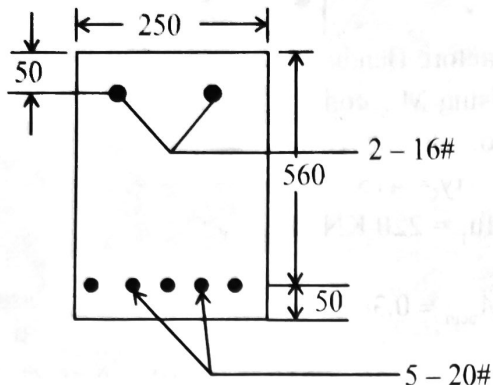
provide 20 mm bar 5nos.

$$\text{So } A_{st \text{ provided}} = 1570 \text{ mm}^2$$

$$A_{sc} = 20 \text{ mm}^2$$

Provide 16 mm bar 2 nos.

$$A_{sc} = 402 \text{ mm}^2$$



- (c) Design a two-way restrained slab for an office floor carrying a live load of 2.5 kN/m^2 . The slab is $4.5 \text{ m} \times 5.5 \text{ m}$ from centre to centre of beam and two adjacent edges are discontinuous. Use M_{15} cone and mild steel bars.

Ans. Room size = $4.5 \text{ m} \times 5.5 \text{ m}$

$$L_x = 4.5 \text{ m}$$

$$L_y = 5.5 \text{ m}$$

Load calculation

Assume thickness of the slab = 150 mm

effective depth of slab = $150 - 20 = 130 \text{ mm}$.

$$\text{Dead load} = 0.13 \times 25 = 3.25 \text{ KN/m}^2$$

$$\text{Live load} = 2.5 \text{ KN/m}^2$$

$$\text{Flwr finish} = 1.0 \text{ KN/m}^2$$

$$\text{Total load} = 6.75 \text{ KN/m}^2$$

$$\text{Factor load} = 1.5 \times 6.75 = 10.125 \text{ KN/m}^2.$$

Moment Calculation

$$M_x = \alpha_x w l_x^2$$

$$M_y = \alpha_y w l_y^2$$

$$\frac{L_y}{L_x} = \frac{5.5}{4.5} = 1.2 < 2$$

Cond. - two adjacent edges are discontinuous

$$\alpha_x = -0.053 = +0.040$$

$$\alpha_y = 0.047 = +0.035$$

Short direction

$$M_x = (-Ve) = 0.053 \times 10.125 \times (4.5)^2 = 10.80 \text{ KN.m}$$

KN.m

$$= (+Ve) = 0.004 \times 10.125 \times (4.5)^2 = 8.20 \text{ KN.m}$$

Long direction

$$M_y = (-Ve) = 0.047 \times 10.125 \times (4.5)^2 = 9.63 \text{ KN.m}$$

kNm.

$$= (+Ve) = 0.035 \times 10.125 \times (4.5)^2 = 7.17 \text{ KN.m}$$

Steel Calculation

$$\frac{M_x}{bd^2} = \frac{10.86 \times 10^6}{1000 \times (130)^2} = 0.8$$

$$P_t = 0.29$$

$$A_{st} = 377 \text{ mm}^2. \text{ Use } 8 \text{ mm at } 120 \text{ mm c/c}$$

Long direction

$$\frac{M_y}{bd^2} = \frac{9.63 \times 10^6}{1000 \times (130)^2} = 0.55$$

$$P_t = 0.265$$

$$A_{st} = 344.5 \text{ mm}^2$$

$$\text{Spacing} = \frac{\text{Area of 1 bar} \times 1000}{344.5} = 145.13$$

use $8 \text{ mm @ } 140 \text{ mm C/C}$.

Check For Deflection

$$\text{Basic } \frac{\text{Span}}{d} = 20$$

$$\frac{\text{Span}}{d} = \frac{4.5}{130} = 34 < \text{Basic}$$

There fore the assumed depth ratio is enough.

6. (a) What are the advantages of two way slab over one way slab.

Ans. One way slab

1. The slab supported in two opposite supports is a one way slab.

2. If $\frac{I_y}{I_x} \geq 2$ is a one way slab.

I_y = Long or length.

I_x = Shorter length.

3. Bending moments deflection are more two way slab.

Two way slab

1. The slab supported on all four edges.

2. $\frac{I_y}{I_x} < 2$ is two way slab.

3. Bending moment and deflection are considerable reduced.

- (b) A.R.C. beam has an effective depth of 500 mm and a breadth of 350 mm. It contains 4-25 mm bars. Calculate the shear reinforcement heeded for a factored shear force of 350 kN. Adopt limit state method and design and assume M 15 grade of concrete and Fe 415 grade of steel.

Ans. $d_{eff} = 500$ m, $b = 350$ mm

$$A_{st} = 4 \times \frac{\pi}{4} \times 25^2 = 1962.5 \text{ mm}^2$$

$$S_u = 350 \text{ KN}, M_{15} \text{ and Fe}_{415}$$

$$\tau_v = \frac{S_u}{bd} = \frac{350 \times 10^3}{350 \times 500} = 2 \text{ N/mm}^2$$

Percentage of steel

$$= \frac{A_{st}}{bd} \times 100 = \frac{1962.5}{350 \times 500} = 112\%$$

For 1.12% $\tau_c = 0.64$

$$\tau_v > \tau_c$$

Shear resisted by concrete = $\tau_v \cdot bd = 0.64 \times 350 \times 500 = 112000 \text{ N} = 112 \text{ KN}$.

Shear to be resisted by stirrup = $S - \tau_c \cdot bd = 350 - 112 = 238 \text{ KN}$.

Provide 2 legged 6 mm diameter stirrup

$$S_v = \frac{.87 f_y \times A_w \times d}{V_{as}} = \frac{.87 \times 415 \times 500 \times A_w}{238 \times 10^3}$$

$$= \frac{.87 \times 415 \times 500 \times 2 \times 28}{238 \times 10^3} = 42.5 \text{ mm}$$

Spacing of stirrup at least of the following.

- (i) 42.5 mm (ii) $75 \times d = 75 \times 500 = 375 \text{ mm}$
 (iii) 300 mm

$$(iv) \frac{A_w f_y}{0.4} = \frac{(2 \times 28) \times 415}{0.4 \times 350} = 166 \text{ mm}$$

use 2 legged 8 mm stirrup at 40 mm c/c.

- (c) Design a slab for a room measuring 5.5×4 m assuming superimposed load of 3 kN/m^2 . The slab is supported on 300 mm thick walls on all four sides and is simply supported at edges with no provision to resist torsion at corners.

HYSD reinforcement of grade Fe 415 L.S.M. of design.

Ans. Short span between centre of bearing = $5.5 + .3 = 5.8 \text{ m}$.

Long span between centre of bearing = $4 + 0.3 = 4.3 \text{ m}$.

Assuming 0.3% of steel, modification factor = 1.43

$$\text{Effective depth required} = \frac{\text{short span}}{20 \times \text{mod factor}}$$

$$\frac{4.3 \times 1000 \text{ mm}}{20 \times 1.43} = 150.3 \text{ mm}$$

Provide 8 mm diameter bar at a clear cover off 15 mm.

$$\text{Effective cover} = 15 + 4 = 19 \text{ mm}$$

$$\text{Overall depth required} = 150.3 + 19 = 169.3 \text{ mm}$$

$$\text{Provide overall depth} = 170 - 19 = 151 \text{ mm}$$

Actual effective depth for short span = $151 - 8 = 143 \text{ mm}$

Effective length should be provided for short span

(i) 4.3 m

(ii) clear span + effective depth = $4 + 0.151 =$

4.151 m.

$$\text{use } L_x = 4.151 \text{ m}$$

$$r = \frac{L_y}{L_x} = \frac{5.643}{4.151} = 1.36$$

Referring is - 456 - 2000

$$\alpha_x = 997, \alpha_y = .053$$

Loads

$$\text{Dead load} = 25 \times 170 = 4250 \text{ N/m}^2$$

$$20 \text{ mm floor finish} = 24 \times 20 = 480 \text{ N/m}^2$$

$$\text{Live load} = 3000 \text{ N/m}^2$$

$$\text{Total load} = 7730 \text{ N/m}^2$$

$$\text{Factored load} = 1.5 \times 7730 = 11595$$

Maximum short span B.M for metre width

$$M_{ux} = \alpha_x w_u .l_x^2 = .09997 \times 11595 \times 4.151^2 = 19919.2 \text{ N}$$

$$M_{uy} = 0.053 \times 11895 \times 4.151^2 = 10589 \text{ Nm}$$

Check for depth

$$d = \sqrt{\frac{M_{ax} \text{ B.M}}{0.138 b \times f_{ck}}}$$

$$= \sqrt{\frac{19919.2 \times 10^3}{138 \times 1000 \times 20}} = 84.95 \text{ mm} < 151 \text{ mm}$$

Percentage of steel

$$\frac{M_x}{bd^2} = \frac{19019.2 \times 10^3}{1000 \times 151^2} = 0.874$$

Percentage of steel from S.P - 16

Page 47 = 26

$$26 = 100 \frac{A_{st}}{bd}$$

$$A_{st} = \frac{26}{100} \times 1000 \times .151 - 3926 \text{ mm}^2$$

use 8 mm bar

$$\text{spacing} = \frac{\text{Area of bar} \times 1000}{\text{Total area}}$$

$$= \frac{50 + 1000}{392.6} = 127.3 \text{ mm}$$

use 8 mm bar at 125 mm C/C.

$$\frac{M_{uy}}{bd^2} = \frac{10589 \times 10^3}{1000 \times 43^2} = 52\%$$

Percentage of steel from sp. 16, page 47 = 146.

$$P = 100 \frac{A_{st}}{bd}$$

$$A_{st} = \frac{146 \times 1000 \times 143}{100} = 208.78 \text{ mm}^2$$

use 8 mm bar

$$\text{spacing} = \frac{\text{Area of 1 bar} \times 100}{\text{Total area}}$$

$$= \frac{50 \times 1000}{208.78} = 239.48 \text{ mm}$$

use 8 mm bar at spacing of 200 mm.

Check for shear

$$V_u = \frac{w \times l_x}{2} = \frac{11595 \times 4.151}{2} = 24065.4 \text{ N}$$

$$\tau_v = \frac{V_u}{bd} = \frac{24065.4}{100 \times 151} = .159 \text{ N/mm}^2$$

$K = 1.3$ (I.S 456 - 2000 calcuse 40.2%)

$$\frac{100A_{st}}{bd} = \frac{100 \times 208.78}{1000 \times 151} = 0.138$$

$$\tau_c = 28$$

$$K \times \tau_c = 1.3 \times 28 = 364 \text{ N/mm}^2$$

$$\tau_v < \tau_c \text{ (so safe)}$$

Check for deflection

$$\frac{\text{Span}}{d} = 20 \text{ (Is 456(23.2.1))}$$

Percentage along $I_x = 26$

$$\text{Allowable } l/d \text{ ratio} = 20 \times 2.85 = 57(\text{sp} - 16)$$

$$\frac{\text{Actual span}}{\text{Depth}} = \frac{4000}{170} = 23.5$$

Allowable 7 actual ok.

7.(a) Mention the value of partial safety factor for concrete and steel.

Ans. The partial safety factor for concrete is 1.5 and for steel is 1.15.

(b) What are the assumptions made in the design for flexure in working stress method ?

Ans. Assumption in working stress methods are

1. Plane section traverse to the centre of line of a member before bending remain plane section after bending.
2. Elastic modulus of concrete has the same value within the limits of deformation of the member.
3. Elastic modulus of steel has same value withing the limit σ_f of the deformation σ_f member.
4. The reinforcement does not slip from concrete surrounding.
5. Steel is free from intial stresses.
6. There is no resultant thrust on any transverse section of the member.

(c) A short RCC column has to carry an axial factored load of 2000 kN. Design the column by using M_{15} grade conc and m.s. reinforcement.

Ans. Axias load = 2000 KN.

Assume $e_{min} < 05 \times D$

But $e_{min} = 20 \text{ mm}$

Therefore the min side of the colⁿ

$$= \frac{20}{0.50} = 400 \text{ mm}$$

colⁿ size = 400×400

Assume 0.8% steel.

$$A_{sc} = 0.008 A_g$$

$$A_c = A_g - A_{sc} = 0.992 A_g$$

$$P_u = 0.4 f_{ck} A_c + 0.67 f_y A_{sc}$$

$$\Rightarrow 2000 \times 10 = (0.4 \times 15 \times 0.992 A_g) + (0.67 \times 250 \times 008 A_g)$$

$$= 5.952 A_g + 1.34 A_g$$

$$= 7.292 A_g$$

$$\Rightarrow A_g = 274273 \text{ mm}^2$$

So one side of the column = 530 mm.

i.e. size of the colⁿ = 530×530

$$P_u = 0.4 f_{ck} A_c + 0.67 f_y A_{sc}$$

$$\Rightarrow 2000 \times 10^3 = \{0.4 \times 15\}$$

$$(530 \times 530 - A_{sc}) + (0.67 \times 250 \times A_{sc})$$

$$= 1685400 - 6 A_{sc} + 167.5 A_{sc}$$

$$\Rightarrow A_{sc} = 1948 \text{ mm}^2$$

$$A_c = (530 \times 530) - 1948$$

$$= 278952 \text{ mm}^2$$

$$A_{sc} = 1948 \text{ mm}^2$$

$$\text{Provid} = 8 - 20\phi \text{ Asc provid} = 2513 \text{ mm}^2$$

Lateral ties.

Use 6mm ϕ lateral ties

Spacing should not exceed

(i) 530 mm

(ii) $16\phi = 16 \times 20 = 320 \text{ mm}$

(iii) 300 mm

(iv) $48 \times 6 = 288 \text{ mm}$

So 6 mm ϕ ties at 280 C/C.

PRACTICE SETS

SET - 1

[CET - 501]

Full Marks - 70

Time - 3 Hours

Answer any five questions.

Figures in the right-hand margin indicate marks.

1. (a) What is the minimum shear stress that can be taken care of by the provision of minimum shear reinforcement provided as per IS 456? [2]
- (b) Bond and Anchorage [5]
- (c) A singly reinforced beam has to carry a maximum bending moment of kN-m. It has a width of 230 mm. Obtain the depth of the beam and area of reinforcement required in tension side. Use M_{20} and mild steel. Adopt working stress method. [7]
2. (a) Write down the functions of stirrups in beams. [2]
- (b) Shear reinforcement [5]
- (c) A beam of size 250 mm × 500 mm in section, is reinforced with two 12 mm Φ bars on compression side and four 20 mm Φ bars on tension side. The bars are at 50 mm centres respectively from bottom and top edge of the beams. Calculate the moment of resistance of the beam, if $Q_{bc} = 7\text{N/mm}^2$, $Q_{st} = 140\text{N/mm}^2$, $Q_{sc} = 230\text{N/mm}^2$ and $m = 13.33$ [7]
3. (a) Find out the anchorage length in tension in a single mild steel bar of dia ϕ in concrete of grade M 20. [2]
- (b) Torsion reinforcement in two-way slab

$$\text{The moment accompanied by torsion } T = \frac{E14\delta}{l_x^2}$$

[5]

- (c) A simply supported one way slab for an office building of a clear span 3m is supported over beams of 240 mm width. Design the slab for a live load of 4 kN/m. The materials used are M20 concrete and HYSD Fe 415 steel. [7]

4. (a) What is the minimum strain in the concrete at the outermost compression fibre in bending as per LSM? [2]
- (b) A rectangular beam 200 mm × 400 mm effective depth is reinforced with three nos. 16 mm bars at bottom and two nos. 10 mm bars at top. The materials are M 20 grade concrete and HYSD grade Fe 415 steel. Cover to compression reinforcement at top is 40 mm and the section is subjected to a moment of 40 kNm. Using WSM, find out the maximum stress in concrete and steel. [5]
- (c) A simply supported rectangular beam section 230 mm wide × 440 mm effective depth is reinforced with 6 × 16 bars at bottom. It is subjected to a factored shear of 200 kN at support. Design the shear reinforcement at support it.
 - (i) all the bars are carried into support.
 - (ii) two nos. 16 mm bars are curtailed at 500 mm from support and
 - (iii) two nos, 16 mm bars are bent at 625 mm from face of support. The ends are confined by compression. M20 concrete and Fe 415 HYSD steel used. [7]
5. (a) Define effective depth and depth of neutral axis. [2]
- (b) Design a simple supported singly reinforced beam of 230 mm wide which carries a factored load of 30 kN/m including its self weight. The flexure and shear by limit state method if materials are M_{15} conc and HYSD bars of Fe415. [5]
- (c) A singly reinforced rectangular concrete beam has to resist an ultimate moment of 90 kN-m. Design the section if for some reasons (a) depth of neutral axis is to be restricted to 0.3 d or (b) $M_u = 1.785 bd^2$. Assume $b = 300\text{ mm}$, $F_{ck} = 15\text{ N/mm}^2$ and $f_y = 415\text{ N/mm}^2$. [7]

6. (a) Calculate development length of Fe415 steel and M_{25} conc. [2]
- (b) Design the sections, for an axially loaded RCC column in the method of Limit State Design. Given data $P_u = 2100$ kN, M_{20} Fe 415. [5]
- (c) A single room measures 4.25 m \times 6.5 m. It is supported on 350 mm thick walls on all four sides. The slab is simply supported at edges. Design the slab using grade M20 concrete and HYSD reinforcement of grade Fe 415. [7]
7. (a) What is the role of concrete cover over the reinforcement? [2]
- (b) A short RCC column of size 400 mm \times 400 mm has to carry an axial factored load of 2000 kN. Assuming $l_{min} < 0.05 D$, design the column using M20 grade of concrete and HYSD grade of steel Fe 415. [5]
- (c) Design a simply supported slab for a span 3.5 m to carry live load of 2 kN/m² and floor finish of 0.75 kN/m². Width of supporting walls is 250 mm. Concrete and steel grades used are M_{20} and Fe₄₁₅ respectively. Adopt Limit State Design Method. [7]

SET - 2

[CET - 501]

Full Marks - 70

Time - 3 Hours

Answer any five questions.

Figures in the right-hand margin indicate marks.

1. (a) Calculate the modular ratio for concrete of grade M_{25} . [2]
- (b) Design a short circular column to carry an axial load working load of 1400 kN by using lateral ties. Assume minimum eccentricity as less than $0.05D$. The materials used are M20 grade concrete and HYSD reinforcement of grade Fe 415. Use 8 mm mild steel bars for lateral ties. [5]
- (c) Design a short column rectangular in section, to carry an axial load of 2200 kN using Fe₄₁₅ and M_{20} . Adopt LSM design. Assume the unsupported length as 3.00 m. [7]

- (i) Longitudinal Reinforcement. [7]
- (ii) Transverse REinforcement [7]
- (iii) Reinforcement details. [7]
2. (a) What is the code provision of stripping time for removal of props to slabs? [2]
- (b) A simply supported slab of clear span 2.6 m is supported on 350 mm thick brick wall at one end and on 230 mm thick brick wall at the other. Loads on the slab are 1 kN/m² floor finish and 2 kN/m² live load. The materials are M_{20} and Fe₄₁₅. Adopt LSM of design. [5]
- (i) Design for flexure and distribution steel. [5]
- (ii) Check for shear, development length and deflection. [5]
- (iii) Reinforcing details as per SP 34. [5]
- (c) Design a rectangular beam simply supported over a clear span of 6 m, if superimposed load is 25 kN/m and support width is 30 cm each. Use M_{15} and Fe₄₁₅. Adopt LSM of design : [5]
- (i) Design for flexure [5]
- (ii) Design for shear [5]
- (iii) Check for development length and deflection. [5]
- (iv) Reinforcing details as per SP 34. [7]
3. (a) Why over reinforced design section is not preferred. [2]
- (b) A T-beam floor consists of 15 cm thick R.C slab monolithic with 30 cm wide beams. The beams are spaced at 3.5 m centre to centre and their effective span is 6 m. If the superimposed load on the slab is 5 kN/m², design and intermediate beam (Reinforcement area only). [5]
- Adopt L.S.M. of design. [5]
- (c) A single room measures 4.25 m \times 6.5 m. It is supported on 350 mm thick walls on all four sides. The slab is simply supported at edges. Design the slab using grade M20 concrete and HYSD reinforcement of grade Fe 415. [7]
4. (a) Write down the minimum eccentricity mentioned in code practice for axially loaded column. [2]
- (b) Draw the idealized stress-strain curve for mild steel bar and HYSD bars, used in limit state method and design. [5]
- (c) A 5 m long simply supported beam carries a superimposed load of 20 kN/k. Design the midspan section if its effective depth is kept constant at 500 mm using. [5]

Figures in the right-hand margin indicate marks.

- (i) Working stress method.
(ii) Limit state method.
and compare the results.
Neglect self weight of the beam
Adopt M20 grade of concrete and Fe 4/5 grade of steel. [7]
5. (a) Write at least two conditions for termination of tension reinforcement in flexural members. [2]
(b) Show that the limiting depth of neutral axis for a rectangular cross-section reinforced with Fe 500 grade steel is $46d$. [5]
(c) A simply supported rectangular beam of 4 m span carries a u.d. of 18 kN/m. The width of the beam is 220 mm. Find out the depth and area of steel required for balanced design by working stress method.
Use - M20 grade of concrete and Fe 415 graded steel. [7]
6. (a) Define the characteristic strength of material. [2]
(b) Calculate the development length for Fe 500 grade of steel and M_{20} of concrete used as a compression member. [5]
(c) Design short column, square in section to carry an axial load of 2000 kN. Adopt L.S method of design and assume Fe 415 grade of steel and M20 mix. [7]
7. (a) What is the maximum permissible diameter of the reinforcing bar for a 130 mm thick R.C.C. slab? [2]
(b) A T-beam of effective flange width 1200 mm, thickness of slab 100 mm, width of rib 300 mm and effective depth of 560 mm is reinforced with 5 no. 25 mm diameter bars. Calculate the factored moment of resistance. The materials are M20 grade concrete and HYSD reinforcement of grade Fe 415. [5]
(c) A rectangular beam of size 230 mm wide \times 565 mm effective depth is subjected to a factored moment 250 kNm. Find the reinforcement for flexure. The material are M20 grade concrete and HYSD reinforcement of grade Fe 415. In case the beam is double reinforced use $d' = 40$ mm. Use LSM. [7]

1. (a) Calculate the effective width of flange for a continuous T beam. $l_{\text{eff}} = 4.5$ m, $b_w = 300$ mm, $D_f = 130$ mm. [2]
(b) Show that the value of neutral axis factor for flexural members by working stress method for balanced section depends only on σ_{st} (permissible stress in steel in tension). [5]
(c) A tee beam of effective flange width of 1800 mm, thickness of slab 100 mm, width of rib 230 mm and effective depth of 500 mm is reinforced with 7 (seven) nos 28 mm diameter bars. The materials are M_{20} and Fe₄₁₅ (Use LSM). [7]
(i) Find actual neutral axis
(ii) Find factored moment of resistance
(iii) Find factored udl inclusive of its own weight assuming simply supported at both ends having effective span 4.5 m.
2. (a) Name the grades of concrete which are used as lean concrete. [2]
(b) A short column of size (230 \times 300) mm is reinforced with 6 nos. of 16 mm dia bars. Determine the safe factored load on column. If the materials are M_{20} conc and HYSD reinforcement of grade Fe415. [5]
(c) A rectangular beam is reinforced with 2 nos of 16 mm dia at top and 3 nos of 20 mm dia at bottom. The beam is 250 mm wide and 460 mm effective depth is subjected to a moment of 60 kN.m. Find out maximum stress developed in materials if M_{20} conc and m.s bar is used. [7]
3. (a) What is the role of concrete cover over the reinforcement? [2]
(b) A simply supported rectangular beam over a span of 3.6 m is reinforced in tension only. The beam is 230 mm wide and had an effective depth of 510 mm. It is reinforced with 4 no. 16 mm diameter bars. Calculate the stresses in both materials at the centre span when the beam carries a uniformly distributed load of 36 kN/m inclusive of self wt. The materials are M20 grade concrete and mild steel reinforcement use WSD method. [5]
(c) A simply supported rectangular beam of 8 m span carries a uniformly distributed load of 23 kN/m,

- inclusive of its self weight. Determine the reinforcement for flexure. The materials are M 30 grade concrete and TMT bars of grade Fe 415, Use LSM. [7]
4. (a) Calculate the flexural strength of which grade of concrete. [2]
- (b) A rectangular R.C.C. beam of size 350 mm width \times 450 mm effective depth is reinforced with 4 nos. 16 mm diameter bars. Find the safe concentrated central point load on a simple span of 3.6 m, which the beam can carry in addition to its self-weight. The materials are M20 grade concrete and HYSD steel of grade Fe 415. Use WSD method. [5]
- (c) A simply supported rectangular beam of 5m span carries a uniformly distributed load 16 kN/m inclusive of its self weight. It also carries a central point load of 16 kN. The width of beam is 230 mm and the materials are M_{20} and mild steel reinforcement (WSM)
- (i) Find the depth.
- (ii) Find the steel area. [7]
5. (a) Where would be the critical section for which shear reinforcement is to be designed if the applied loads introduce tension in the end regions of a beam? [2]
- (b) A simply supported tee-beam of 8m clear span carries a total characteristic load of 30 kN/m. The section of the beam is 230 mm wide \times 500 mm effective depth. It is reinforced with 6 no. of 20 mm diameter bars. design the shear reinforcement using vertical stirrups only. The ends of the beam are confined by compressive reaction. The materials are M20 grade concrete and HYSD steel of grade Fe 415. Use mild steel bar of 6 mm diameter for minimum shear reinforcement. Show different section on the beam by line diagram. Use LSM. [5]
- (c) A simply supported rectangular beam of 6 m span carries a uniformly distributed characteristic load of 24 kN/m inclusive of its self-weight. The beam section is 230 \times 600 mm overall. The materials are M20 grade concrete and HYSD reinforcement of grade Fe 415. Design the beam for flexure and check for development length and deflection. Use LSM. [7]
6. (a) Mention the cases in which you would recommend a double reinforced beam. [2]
- (b) A tee-beam section having 230 mm width of web and 460 mm effective depth is reinforced, with 5 nos. of 16 mm dia bars as tension reinforcement which continue for a distance greater than effective depth, past the section. The section is subjected to a factored shear of 90 kN. Check the shear stresses and design the shear reinforcement. The materials used are M20 grade concrete and HYSD reinforcement of grade Fe 415. Use mild steel bars for stirrups. [5]
- (c) A doubly reinforced rectangular beam of overall size 230 mm width \times 550 mm depth is reinforced with 2 nos. 20 mm diameter bars at top and 4 nos. 20 mm diameter bars at bottom. If this beam is subjected to a moment of 72 kN-m, consider $d = 500$ mm, $d' = 50$ mm. Use M_{20} and Fe_{415} . Adopt working stress method.
- (i) Find the stress in concrete.
- (ii) Find the stress in comp steel.
- (iii) Find the stress in tension steel. [7]
7. (a) Find the required cross-sectional area of column when (i) $M_U = 4000$ kN (ii) Grade = M_{20} Fe_{415} (iii) 1.0% reinforcement. [2]
- (b) A L-beam has a flange of effective width 90 cm and depth 10 cm. Determine the areas of compression and tension steels needed for the cross-section if it is to carry a factored bending moment of 600 kN-m. Assume M_{20} and Fe_{500} and use limit state method.
- (i) For determination of tension steel.
- (ii) For determination of compression steel. [5]
- (c) A short column 400 mm \times 400 mm is reinforced with 4 nos. of 25 mm diameter bars. Find the ultimate load carrying capacity of the column if the minimum eccentricity is less than .05 times the lateral dimensions. The materials are M 20 grade of concrete and Fe 415 grade of steel. Adopt limit state method. [7]

SET - 4

[CET - 501]

Full Marks - 70

Time - 3 Hours

Answer any five questions.

Figures in the right-hand margin indicate marks.

1. (a) Define moment of Resistance. [2]

- (b) Discuss the detailing requirements for reinforcement in a two-way slab with corners held down. [5]
- (c) A short RCC column of size $400 \text{ mm} \times 400 \text{ mm}$ has to carry an axial factored load of 2000 kN. Assuming $l_{\min} < 0.05 D$, design the column using M20 grade of concrete and HYSD grade of steel Fe 415. [7]
2. (a) State reasons why overreinforced section is not allowed in limit state method of design. [2]
- (b) A simply supported rectangular beam ($250 \text{ mm} \times 450 \text{ mm}$) reinforced with 4 nos of 16 mm dia bars as tension reinforcement is subjected to an all inclusive load of 20 kN/m over a span of 3.5 m. Design suitable shear reinforcement. The materials are M20 and Fe 415. [5]
- (c) A RCC column of dimensions $250 \text{ mm} \times 500 \text{ mm}$ is reinforced with (4 – 16 + – 12) bars equally distributed on all sides. Calculate and show the details of transverse reinforcement with the help of a sketch. [7]
3. (a) Mention any two advantages of doubly reinforced beam. [2]
- (b) Establish the comparison between working stress method and limit state method. [5]
- (c) Find the depth of neutral axis of a singly reinforced RC beam of 230 mm width and 450 mm effective depth. It is reinforced with 4 bars of 16 mm diameter. Use M-20 concrete and Fe-415 bars. Use WSM and state type of beam is it. [7]
4. (a) What do you know by M-15 grade of concrete? [2]
- (b) Explain the assumption in LSM of design. [5]
- (c) A singly reinforced concrete beam 250 mm width is reinforced 4 bars of 25 mm diameter at an effective depth of 400 mm. If M-20 grade concrete and Fe-415 bars are used, compute ultimate moment of resistance of the section in LSM. [7]
5. (a) Write the purpose of providing distribution steel in RCC slabs. [2]
- (b) A short RCC column $450 \text{ mm} \times 450 \text{ mm}$ is provided with 8 bars of 16 mm diameter. If the effective length of the column is 2.5 m, find ultimate load for the column. Use M 20 concrete and Fe 415 steel. Solve by LSM method. [5]
- (c) ARCC beam of overall dimensions $250 \text{ mm} \times 400 \text{ mm}$ is subjected to a bending moment of 50 kN-m. Using M20 and Fe 415, design the section by working stress method and show details of reinforcement by a neat sketch. Assume suitable cover for mild exposure condition. [7]
6. (a) Give reasons why over reinforced section is not allowed in limit state method of design. [2]
- (b) A simply supported rectangular beam ($250 \text{ mm} \times 400 \text{ mm}$) reinforced with 5 nos. of 16 mm dia bars as tension reinforcement is subjected to an all inclusive load of 16 kN/m over a span of 5 m. Design for the shear reinforcement by using a combination of bent up bars and vertical stirrups assuming the ends of reinforcement are confined with compressive reaction. The materials are M20 and Fe415. [5]
- (c) A RCC beam of overall dimensions $250 \text{ mm} \times 450 \text{ mm}$ is subjected to a bending moment of 50 kNm. Using Fe 415 and M20 design the section by working stress method of design and show the details of main reinforcement by a neat sketch. Assume suitable cover for moderate exposure condition. [7]
5. (a) What are the codal provisions of stripping time for removal of props to beams? [2]
- (b) A doubly reinforced beam section 250 mm wide and 450 mm deep to the centre of the tensile reinforcement. It is reinforced with 2 bars of 16 mm diameter as compressions reinforcement at an effective cover of 50 mm and 4 bars of 25 mm diameter as tensile steel. Assume M 20 concrete and Fe 415 steel. Calculate moment of resistance of the beam section. [5]
- (c) Design a RCC column of the following specification using LSM.
- Axial factored load = 1800 kN
 - Effective length = 2.25 m
 - Grade of steel = Fe 415
 - Grade of concrete = M 25. [7]